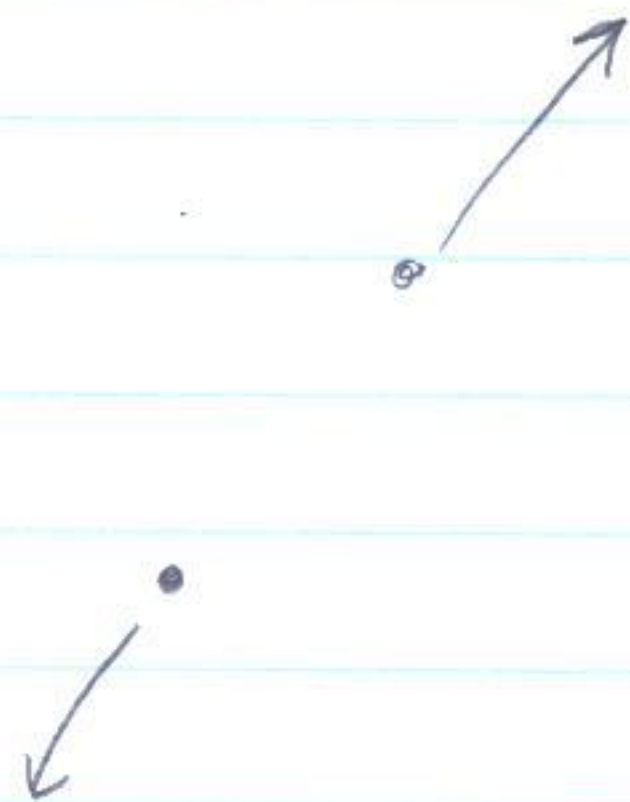


Last time :

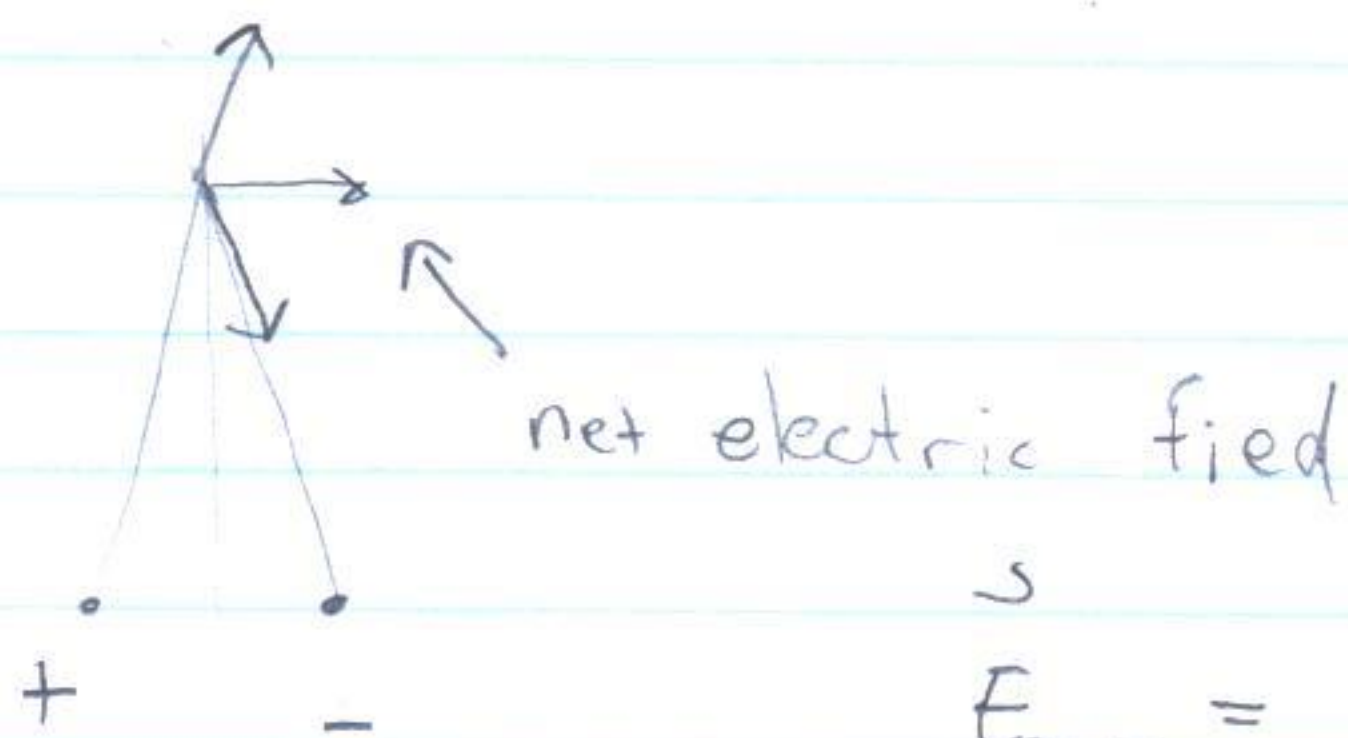
$$\vec{F}_{12} = k_e \frac{q_1 q_2}{r^2} \hat{r}_{12}$$

$\underbrace{\hspace{1.5cm}}_{\frac{1}{4\pi\epsilon_0}}$



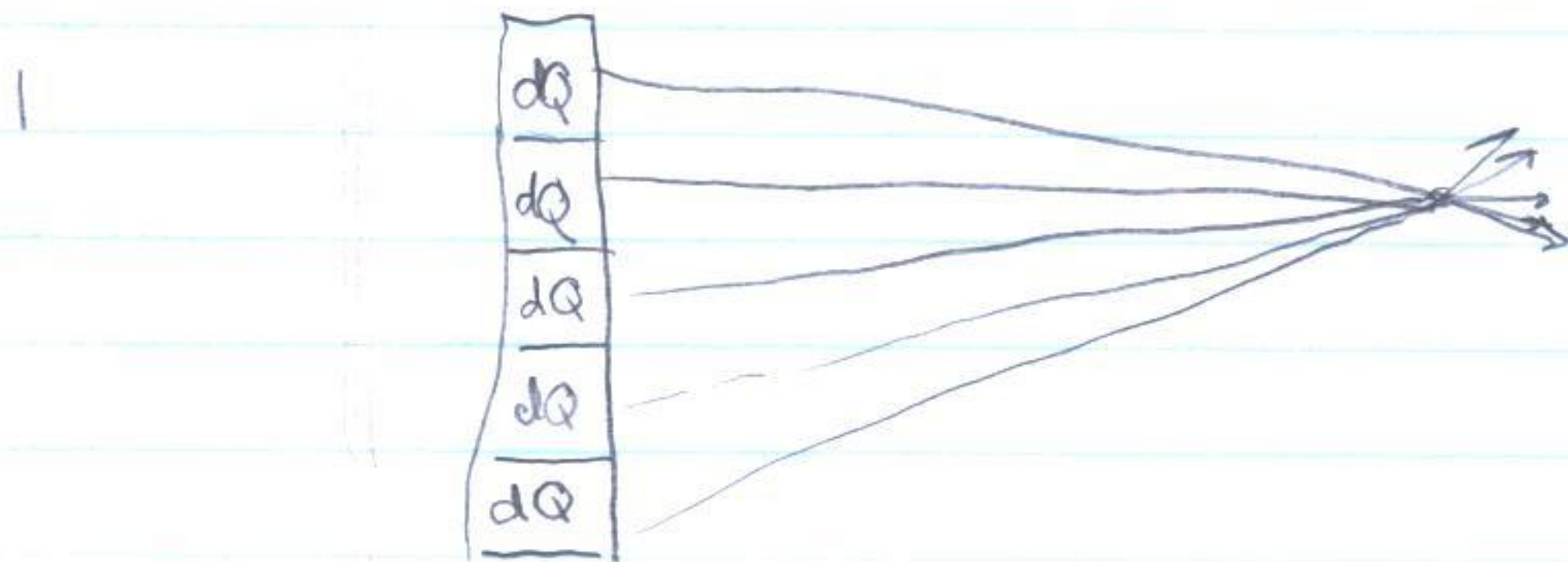
Point Charges

$$\vec{E} = \frac{\vec{F}}{q_0} \longrightarrow \frac{k_e Q}{r^2} \hat{r} \quad (\text{Electric Field From a point charge})$$



$$\vec{E}_{\text{TOT}} = \vec{E}_+ + \vec{E}_-$$

Continuous Distribution :



$$\vec{E}_{\text{TOT}} = \sum_i \vec{E}_i = \sum \frac{dq}{r_i^2} k_e \hat{r}_i$$

Then we had:

$$\lambda = \frac{\text{Charge}}{\text{Length}}$$

$$dQ = \lambda dx$$

$$E_{\text{Tot}} = \sum_i k_e \frac{dQ}{r^2} \rightarrow \int_0^L k_e \frac{\lambda dx}{r^2}$$

A. Last Time Compute Electric Field \mathcal{E}

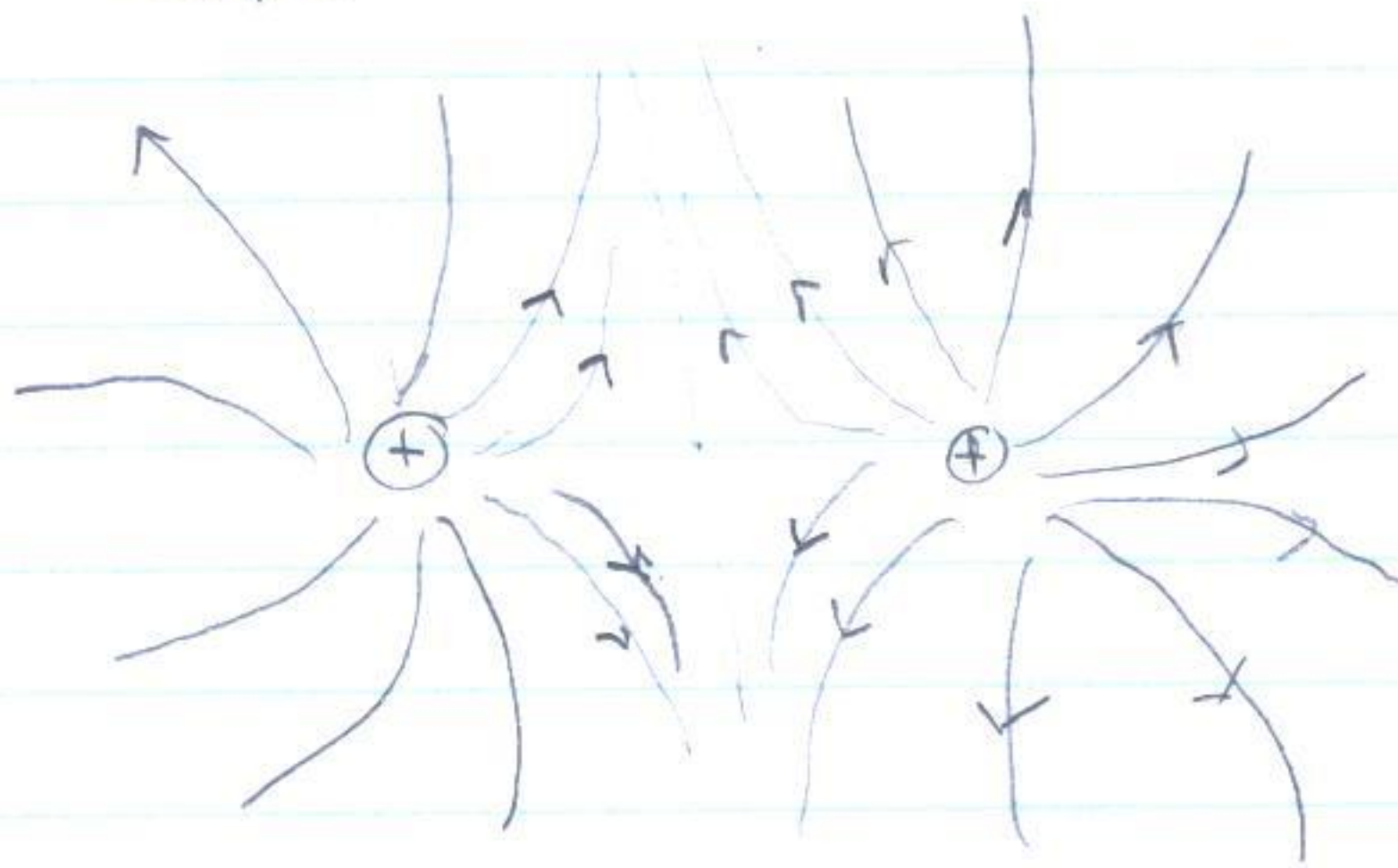
B. Today, What happens when you put a charge in an \mathcal{E} -field

Answer: you move

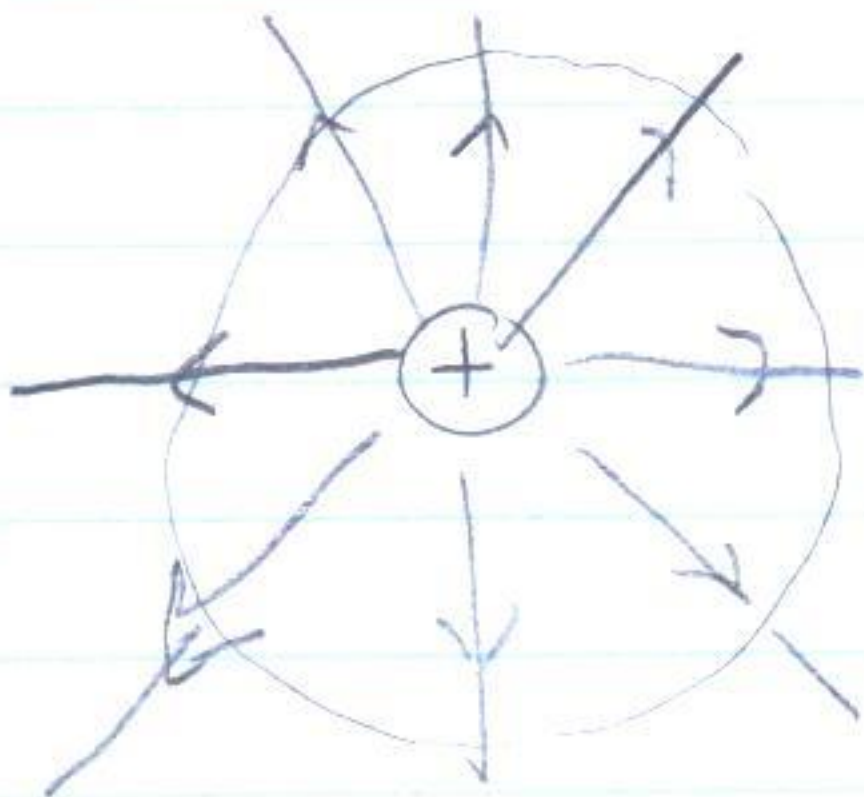
$$\vec{F} = q \vec{E}(x, t) = m \vec{a}$$

- Show Electric Field Applet:

Example



Coulomb Law:



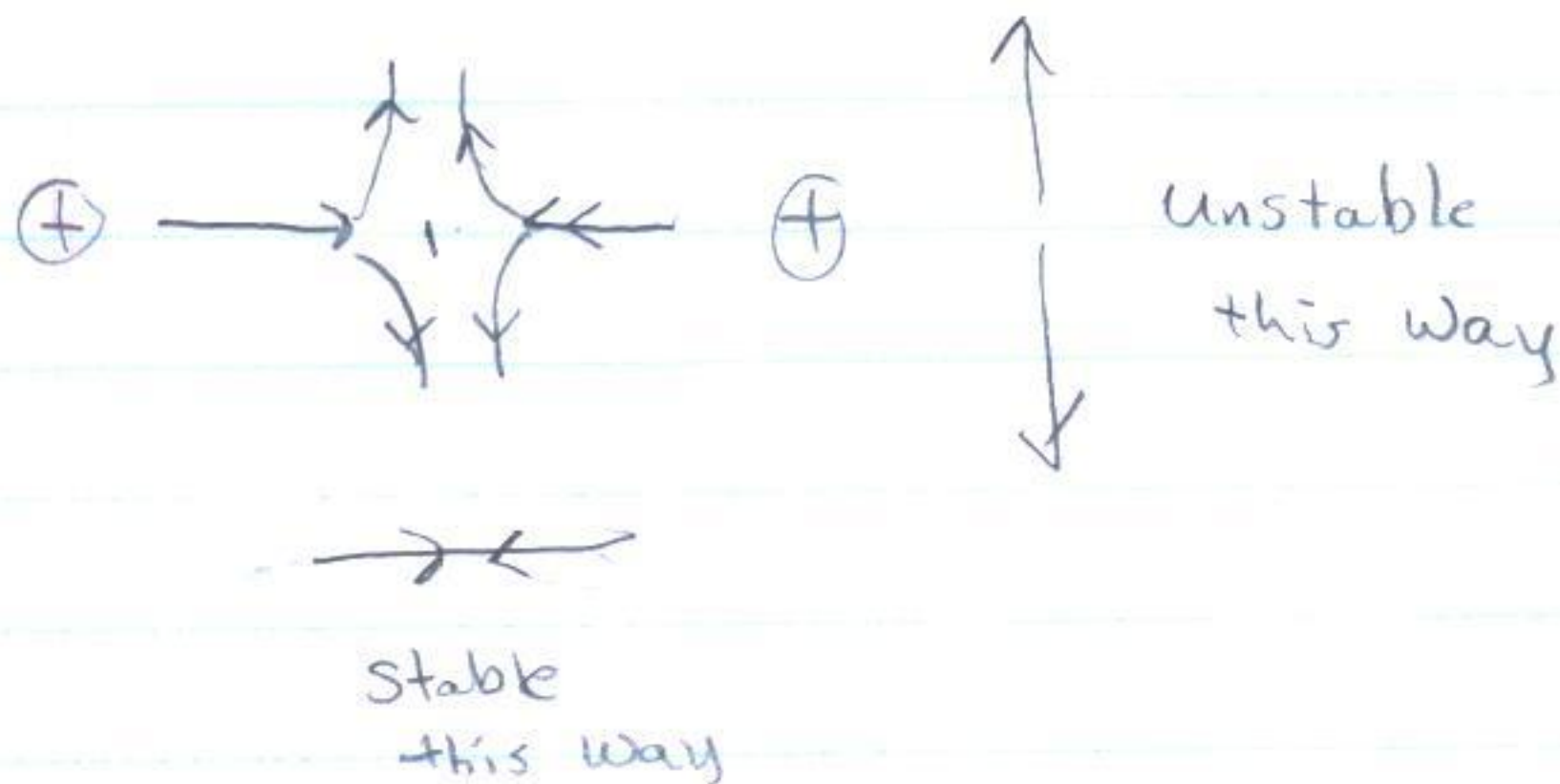
$E \propto$ density of Lines

$$E \propto \frac{N_{\text{lines}}}{4\pi r^2}$$

$$E \propto \frac{1}{r^2}$$

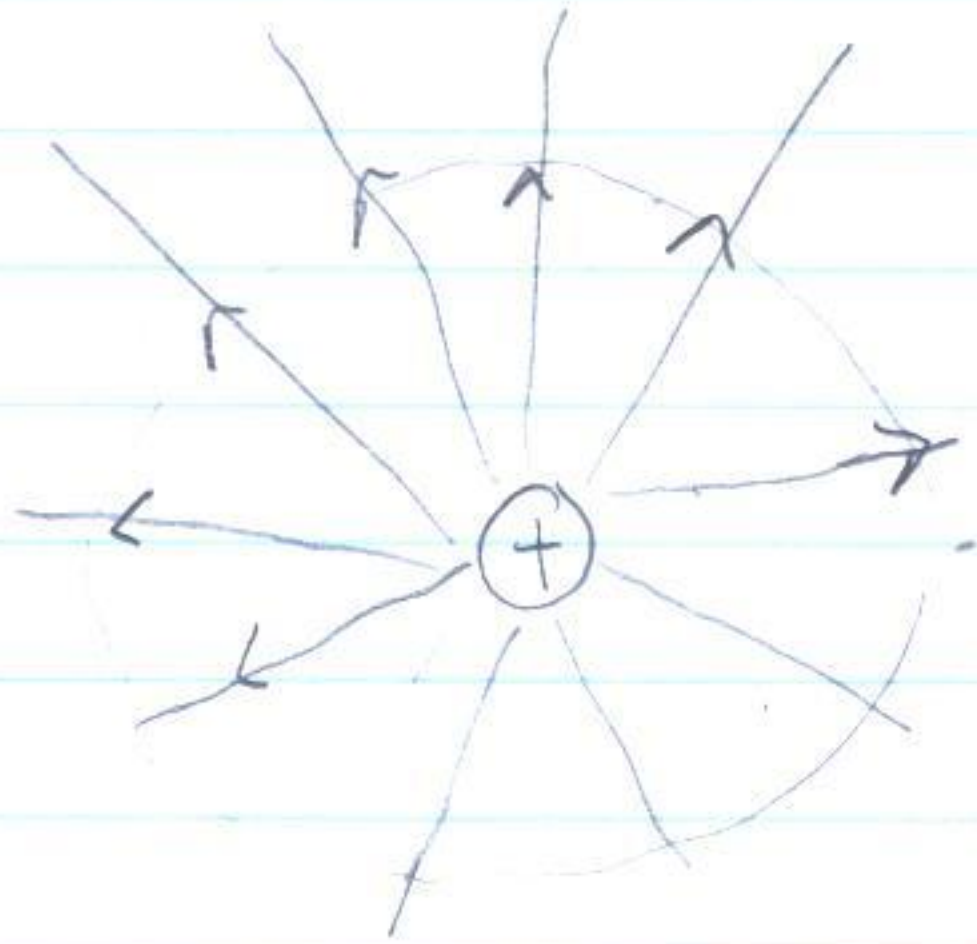
There is no stable Equilibrium?

In order to make stable



lines would have to cross

Electric Field Lines



- Arrows Show The direction of the Field

- Density = # of Lines Crossing / Area = strength of field

- The number of field lines leaving a charge is \propto to charge

- Electric Field lines start on + charges and end on negative charges



- Electric Field lines don't cross

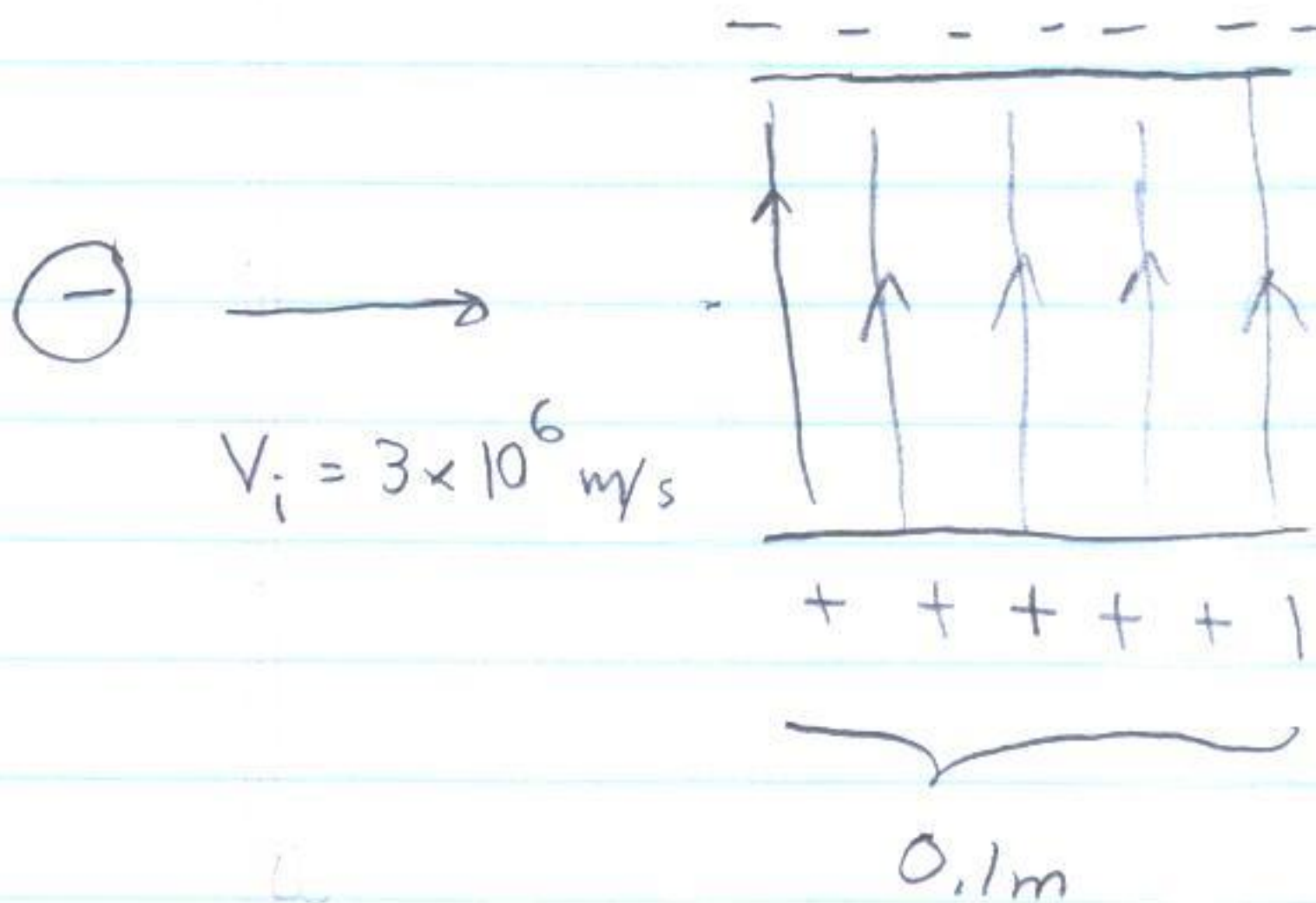
E_{Tot} is a sum

Motion In a constant Field

$$\vec{F} = q \vec{E} = m \vec{a}$$

$$\frac{q}{m} \vec{E} = \vec{a} \quad (A \text{ is constant})$$

Example:



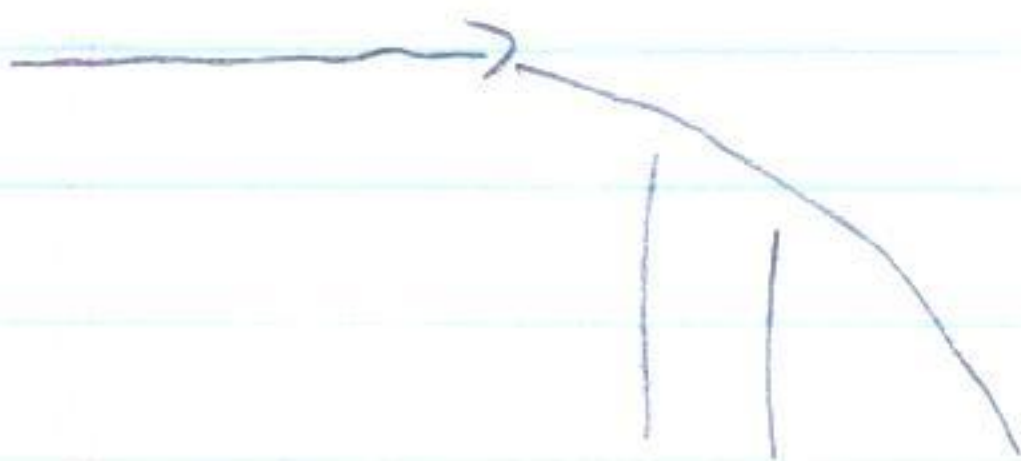
$$E = \frac{200 \text{ N}}{\text{C}} = \frac{200 \text{ V}}{\text{m}}$$

$$E = \frac{200 \text{ V}}{100 \text{ cm}} = \frac{2 \text{ V}}{\text{cm}}$$

(Break Down Air $\sim 10 \text{ kV}$ / cm)

• Constant acceleration down:

$$\vec{a} = \frac{q}{m} \vec{E} = - \frac{|q| |E|}{m} \hat{j}$$



just like a rock thrown from a cliff²

x and y are independent

$$\left. \begin{aligned} x &= x_0 + v_{0x} t + \frac{1}{2} a_x t^2 \\ y &= y_0 + v_{0y} t + \frac{1}{2} a_y t^2 \end{aligned} \right\} \begin{array}{l} \vec{x} \text{ vs. } t \\ \text{const acceleration} \end{array}$$

$$\left. \begin{aligned} v_x(t) &= v_{0x} + a_x t \\ v_y(t) &= v_{0y} + a_y t \end{aligned} \right\} \begin{array}{l} \vec{v} \text{ vs. } t \end{array}$$

Questions when does it reach the end

$$t_f = \frac{L}{v_x} = \frac{0.1 \text{ m}}{3 \times 10^6 \text{ m/s}} = 0.333 \times 10^{-6} \text{ s} = 33 \text{ ns}$$

What is the displacement Δy



$$y(t) = y_0 + v_{0y} t + \frac{1}{2} a_y t^2$$

$$y = \frac{1}{2} - \frac{1}{m} \frac{q|E|}{c} t_f^2$$

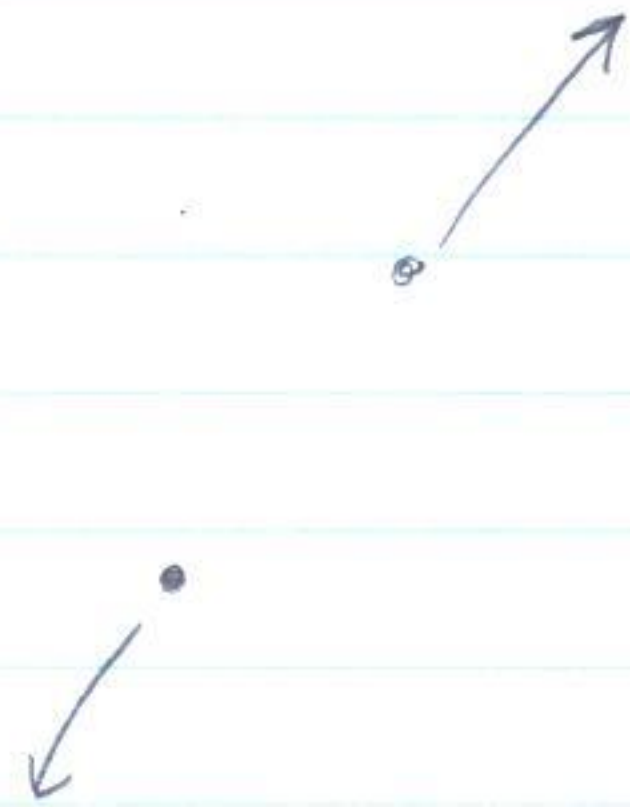
$$q = 1.6 \times 10^{-19} \text{ C}, \quad E = 200 \frac{\text{N}}{\text{C}}, \quad m = 9.11 \times 10^{-31} \text{ kg}$$

$$t_f = 3.33 \times 10^{-8} \text{ s}$$

$$y = -1.95 \text{ cm}$$

Last time :

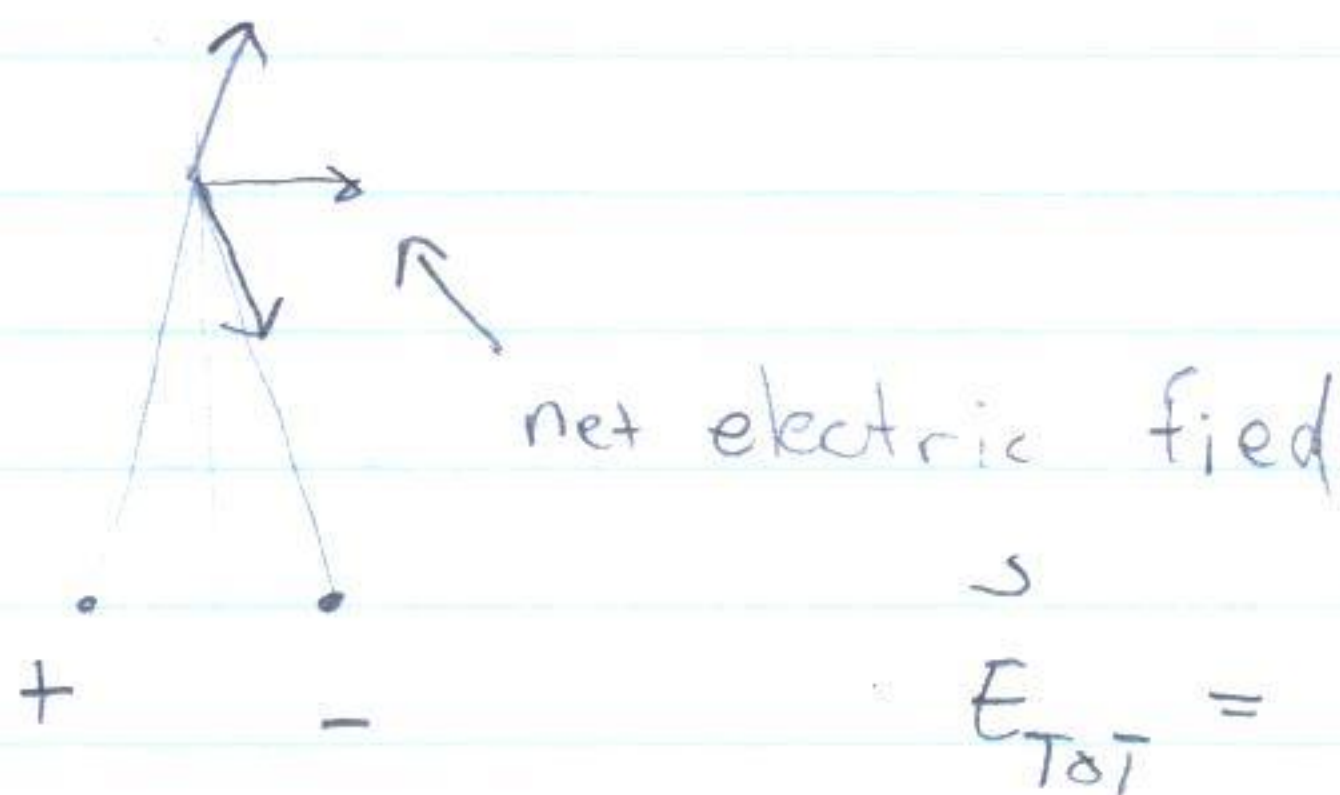
$$\vec{F}_{12} = \underbrace{k_e}_{\frac{1}{4\pi\epsilon_0}} \frac{q_1 q_2}{r^2} \hat{r}_{12}$$



Point

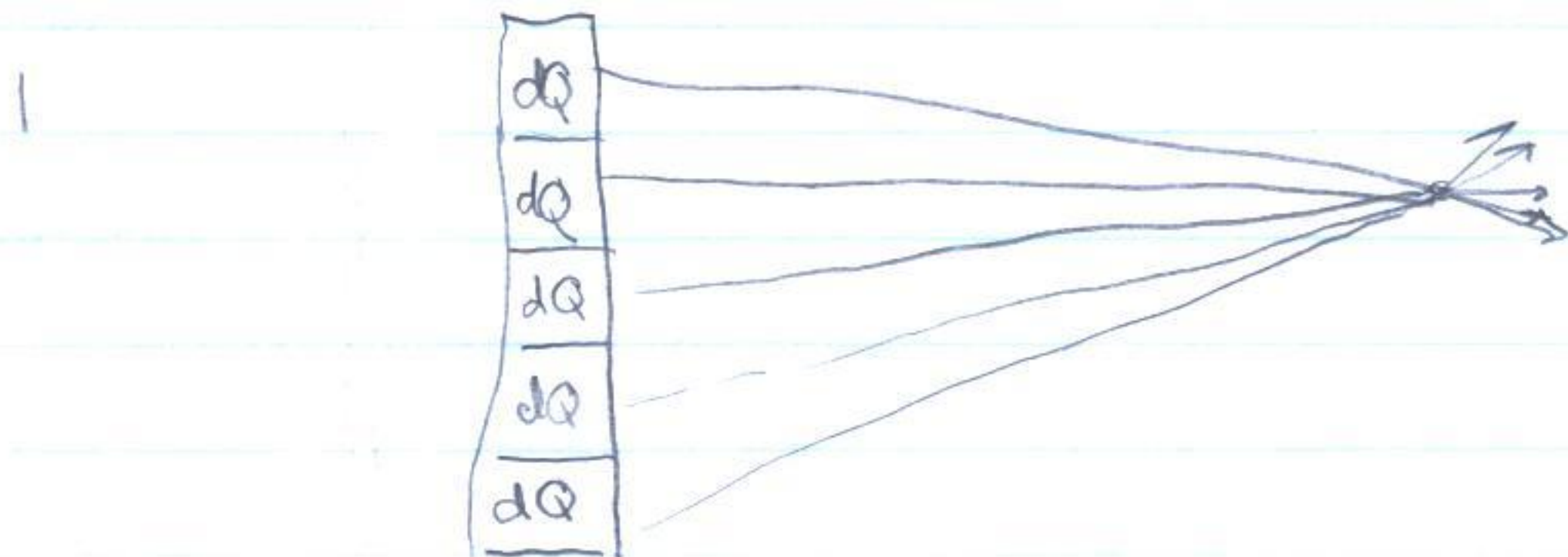
Charges

$$\vec{E} = \frac{\vec{F}}{q_0} \rightarrow \frac{k_e Q}{r^2} \hat{r} \quad (\text{Electric Field From a point charge})$$



$$\vec{E}_{\text{TOT}} = \vec{E}_+ + \vec{E}_-$$

Continuous Distribution :



$$\vec{E}_{\text{TOT}} = \sum_i \vec{E}_i = \sum \frac{dQ}{r_i^2} k_e \hat{r}_i$$