

# What the parton cascade tells us about RHIC

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Workshop on “Collective flow and QGP properties”

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- based on projects with: P. Huovinen, Z. W. Lin, S. A. Voloshin, M. Gyulassy

# Outline

- **Covariant parton transport theory**
  - transport equation & ingredients
- **Elliptic flow ( $v_2$ ) puzzle at RHIC**
  - observation: large and saturating anisotropy  $v_2(p_\perp)$
  - puzzle for models → **large opacities?**
- **Looking for ways out**
  - dynamics? -  $2 \leftrightarrow 3$
  - hadronization? - parton coalescence
- **Did we reach the hydro limit?**

# The theory

# Covariant parton transport theory

Pang, Zhang, Gyulassy, D.M., Vance, Csizmadia, Pratt, Cheng, ...

## Simplest Lorentz-covariant **nonequilibrium** dynamical framework

- dynamics governed by the **mean free path**:  $\lambda(s, x) = 1/\sigma(s)n(x)$ 
  - interpolates between ideal hydro  $\lambda = 0$  and free streaming  $\lambda = \infty$
- **natural decoupling**,  $\lambda(t \rightarrow \infty) \rightarrow \infty \iff$  no need for sudden Cooper-Frye

## Nonlinear 6+1D transport equation:

$$p^\mu \partial_\mu f_i(x, \vec{p}) = \overbrace{S_i(x, \vec{p})}^{\text{source } 2 \rightarrow 2 \text{ (ZPC, GCP, ...)}} + \overbrace{C_i^{el.}[f](x, \vec{p})}^{2 \leftrightarrow 3 \text{ (MPC)}} + \overbrace{C_i^{inel.}[f](x, \vec{p})}^{2 \leftrightarrow 3 \text{ (MPC)}} + \dots$$

solvable numerically  $\rightarrow$  only a few **covariant** algorithms: ZPC, **MPC**, Bjorken- $\tau$ , ...

Real dynamical parameter: **transport opacity** [see NPA 697, 495 ('02)]

$$\chi \equiv \langle n_{coll} \rangle \sigma_{tr} / \sigma_{el} \propto \sigma_{tr} \times dN/d\eta$$

# Three ingredients (for RHIC)

- **initial conditions**

- soft + hard (minijets)
- gluon saturation
- ...

- **cross sections**

- e.g., perturbative QCD (LO) + screening
- ...

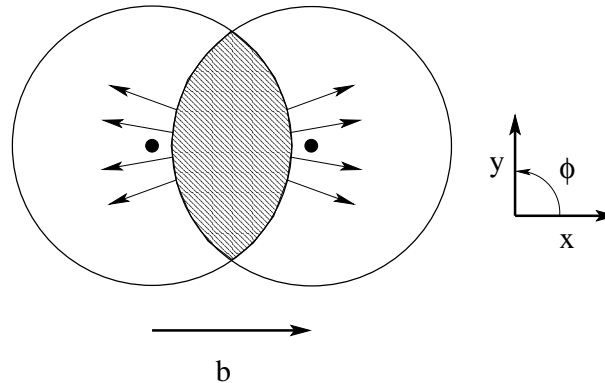
- **hadronization**

- parton-hadron duality (1 parton  $\rightarrow$  1 pion)
- independent jet fragmentation
- Lund string model
- parton coalescence
- ...

# Applications - collective phenomena

# Elliptic flow

- momentum-space **anisotropy** of particle production in A+A collisions

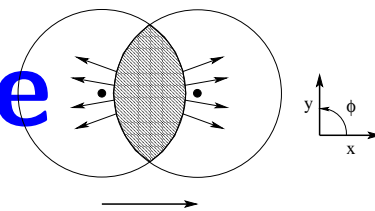


$$\frac{dN}{d\phi dX} \equiv \frac{1}{2\pi} \frac{dN}{dX} \left[ 1 + 2 \sum_{n=1} v_n(X) \cos(n\phi) \right] \quad \rightarrow \quad v_2(X) \equiv \langle \cos 2\phi \rangle_X$$

$X$  : event and particle selection, e.g., centrality, **transverse momentum**

- **origin of  $v_2 \neq 0$** : coordinate-space anisotropy ( $b > 0$ ) & reinteractions

# RHIC elliptic flow puzzle

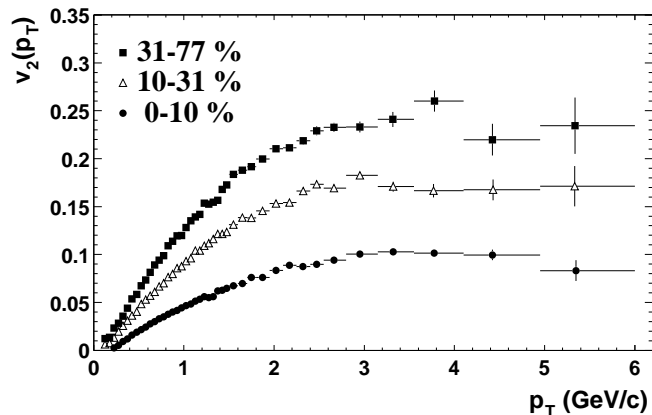


**Experimental data**

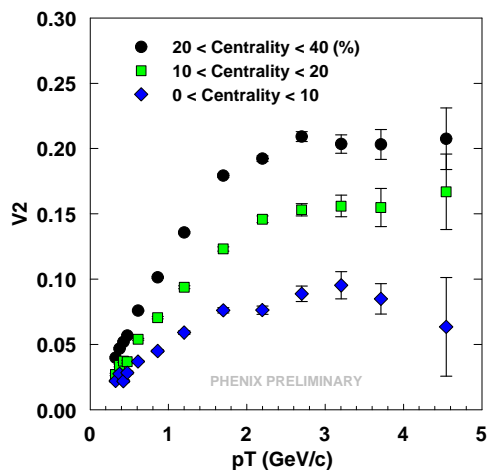
vs.

**Theoretical expectations<sup>b</sup>**

STAR, PRL 90, 032301 ('03)



PHENIX, NPA715, 765 ('03)



• **large and saturating anisotropy  $v_2(p_{\perp})$**

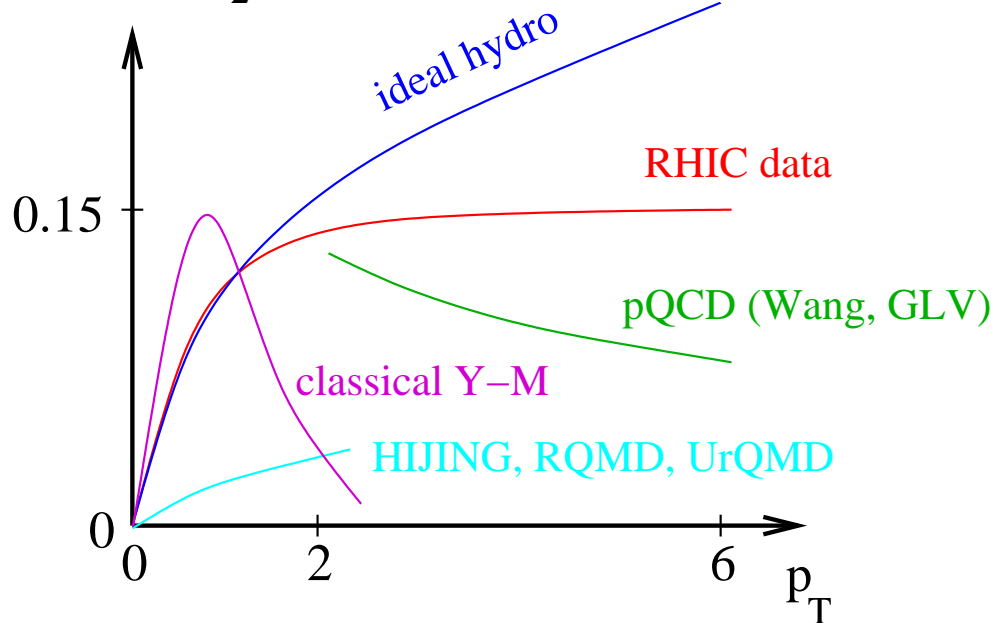
[Heinz, Kolb, Huovinen et al;

Gyulassy, Vitev, Wang et al;

Sorge et al; Bleicher, Stöcker et al;

Krashnitz, Venugopalan et al]

minbias  $v_2$

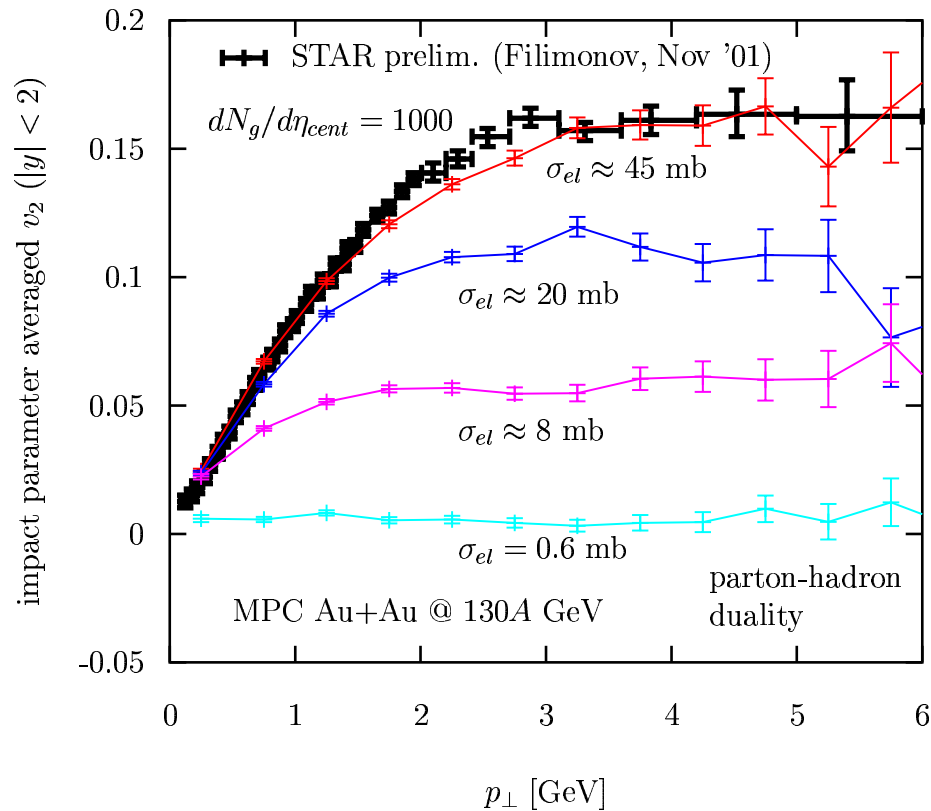


• **difficult to explain**



# $v_2(p_T)$ from parton transport

D.M. & Gyulassy, NPA 697 ('02):



**covariant parton transport model MPC 1.6.0 (D.M.)**

$$p^\mu \partial_\mu f_i = S_i + C_i^{2 \rightarrow 2}[f] + \dots$$

- minijet initconds + gluon sat.
- screened  $2 \rightarrow 2$  pQCD cross sections
- 1 parton  $\rightarrow$  1 pion hadronization

- $v_2$  saturation pattern reproduced with  **$15\times$  enhanced opacities**

$$\sigma_{el} \times dN_g/d\eta \approx 45000 \text{ mb} \gg \text{pQCD (3 mb} \times 1000)$$

**Look for ways out**

# One bet: inelastic processes

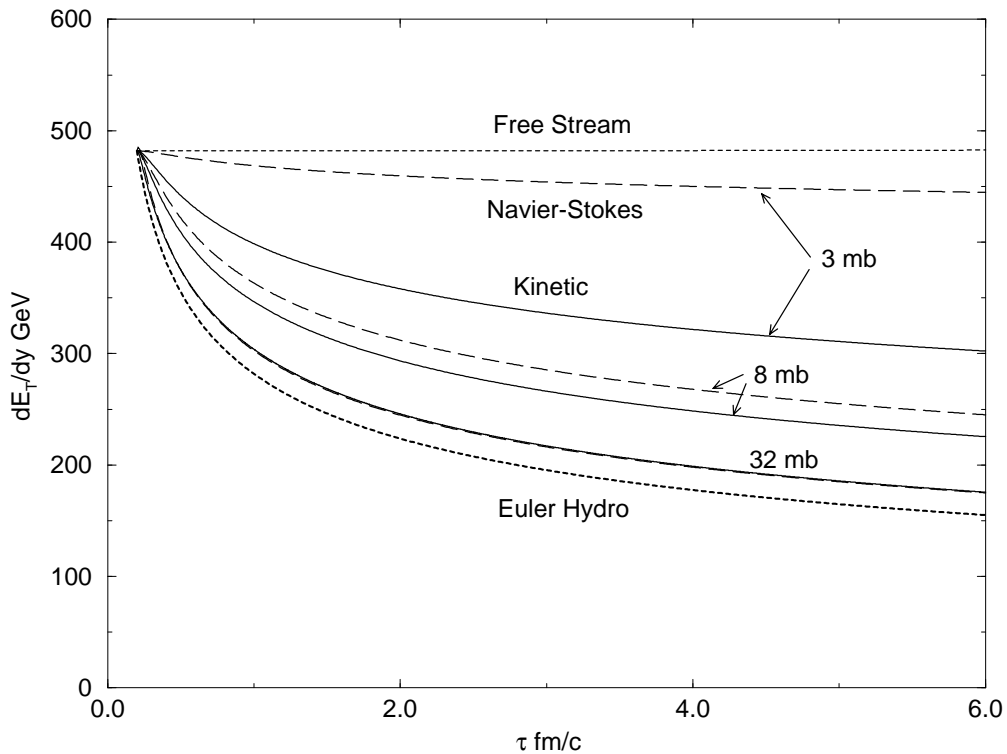
- **hope: opacity enhancement** due to particle production
- **natural step: investigate  $2 \rightarrow 2 + 2 \leftrightarrow 3$** 
  - algorithm for  $3 \rightarrow 2$  has been developed (MPC)
  - but: **several orders of magnitude** larger CPU time required for covariance ( $\ell^{-1/5}$ )
  - unfortunately, full 3+1D simulation for RHIC is unfeasible

⇒ needed to get insight from a **simpler problem (symmetry)**:

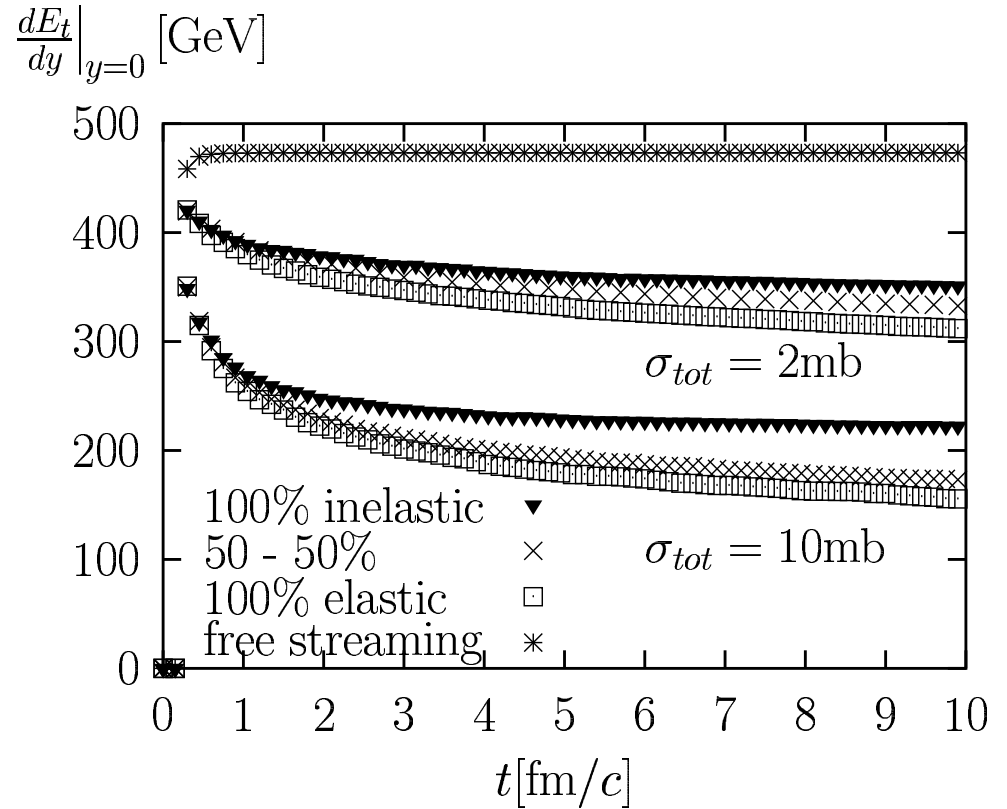
- **choose:  $E_T$  evolution in 1+1D Bjorken scenario**
  - expanding systems cool due to  $p dV$  work
  - $E_T$  reflects  $p dV$  work ⇒ **measures strength of collective phenomena**
  - e.g., **ideal hydro**:

$$T \propto \tau^{-1/3} \quad \Rightarrow \quad dE_T/dy \propto \tau^{-1/3}$$

pure  $2 \rightarrow 2$  (Zhang & Gyulassy):



$2 \leftrightarrow 3$  vs  $2 \rightarrow 2$  (D.M. & Gyulassy):



- $p dV$  work increases with opacity
- demonstrated approach to Navier-Stokes

- elastic and inelastic channels have similar transport effect
- ⇒ effect of  $2 \leftrightarrow 3$  is roughly a doubling of  $2 \rightarrow 2$  cross section

Hope looks gone: there is room for  $2 - 3 \times$  larger opacities but not  $15 \times$

# Another idea: parton coalescence

Biró et al, Lévai, Csizmadia, Ko, Lin, Hwa, Yang, Greco et al, Fries et al, D.M., Voloshin, ...

An alternative to  $1 \rightarrow$  many independent fragmentation

- **picture:** - coalescence of massive “dressed” valence quarks  
- no dynamical gluons
- **basic equations:**  $qq \rightarrow$  meson,  $qqq \rightarrow$  baryon      many  $\rightarrow$  1

$$E \frac{dN_M(\vec{p})}{d^3p} = \int \frac{d\sigma^\mu p_\mu}{(2\pi)^3} \int d^3q |\psi_{\vec{p}}(\vec{q})|^2 f_\alpha(\vec{p}_\alpha, x) f_\beta(\vec{p}_\beta, x)$$

$$E \frac{dN_B(\vec{p})}{d^3p} = \int \frac{d\sigma^\mu p_\mu}{(2\pi)^3} \int d^3q_1 d^3q_2 |\psi_{\vec{p}}(\vec{q}_1, \vec{q}_2)|^2 f_\alpha(\vec{p}_\alpha, x) f_\beta(\vec{p}_\beta, x) f_\gamma(\vec{p}_\gamma, x)$$

hadron yield      space-time      wave-fn.      quark distributions

**assumes:** rare process, weak binding, factorizable 2-body and 3-body density matrix, smooth spacetime distributions, 3D hypersurface (sudden approx.)

- **can dominate over fragm. for  $p_\perp < 4 - 5$  GeV**

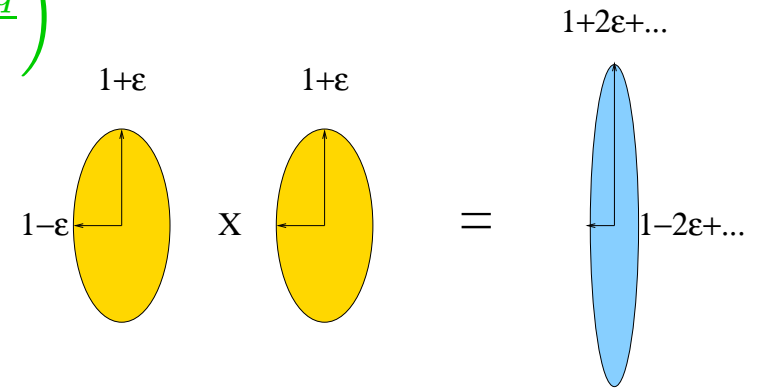
# Coalescence amplifies elliptic flow

[D.M & Voloshin, PRL 91 ('03)]

narrow wave fn. limit ( $\vec{q} = 0$ ):  $\frac{dN_M}{d\phi} \propto \left(\frac{dN_q}{d\phi}\right)^2$

$$v_2^M(p_\perp) \approx v_2^a\left(\frac{p_\perp}{2}\right) + v_2^{\bar{a}}\left(\frac{p_\perp}{2}\right)$$

$$v_2^B(p_\perp) \approx v_2^a\left(\frac{p_\perp}{3}\right) + v_2^b\left(\frac{p_\perp}{3}\right) + v_2^c\left(\frac{p_\perp}{3}\right)$$

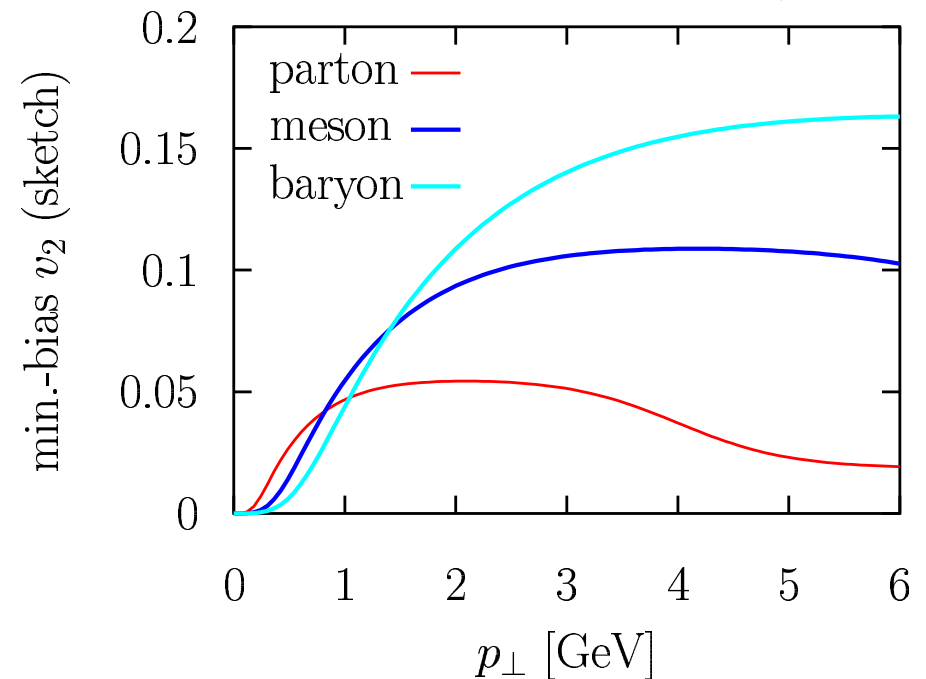


⇒ **hadron flow amplified at high  $p_\perp$**   
if all quarks have same  $v_2$ :

3× for baryons

2× for mesons

“  $v_2^h(p_\perp) \approx n \times v_2^q(p_\perp/n)$  “



• this **KEY EFFECT** solves opacity puzzle (much smaller parton  $v_2$  needed)

# Solution to opacity puzzle

1) elliptic flow amplification  $\Rightarrow 2 - 3 \times$  smaller parton  $v_2$  is enough

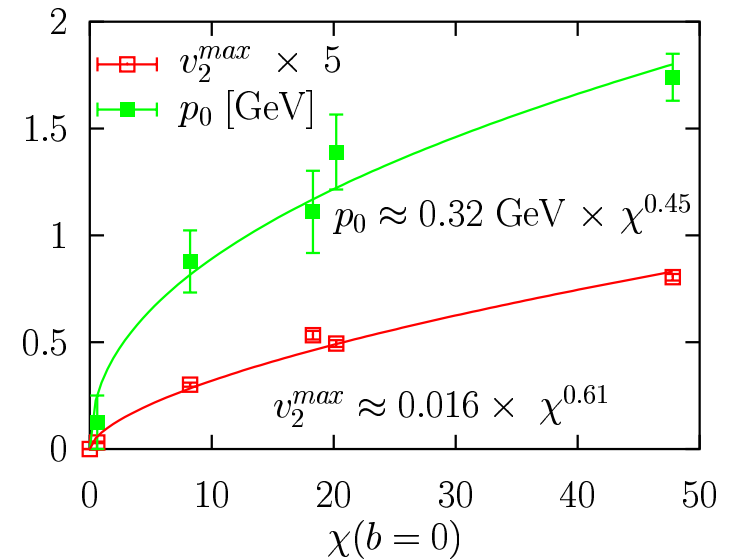
**weaker than linear** opacity dependence

$$v_2^{max}(\chi) \propto \chi^{0.61}$$

$$v_2^{parton}(p_{\perp}, \chi) \approx v_2^{max}(\chi) \tanh(p_{\perp}/p_0(\chi))$$

$\Rightarrow$  3 - 6  $\times$  opacity reduction [ $\chi \sim \sigma \times dN/d\eta$ ]  
[lower(upper) value for purely mesons(baryons)]

[D.M & Gyulassy, NPA 697, 495 ('02)]



2) 15 - 20% nonflow correlations in first  $v_2$  data  $\Rightarrow$  25% opacity reduction

3) theoretical uncertainties  $\Rightarrow$  factor 2 - 3 in opacity [D.M & Gyulassy, NPA 661]  
inelastic processes (e.g.,  $2 \leftrightarrow 3$ ), cross sections, initial parton density, ...

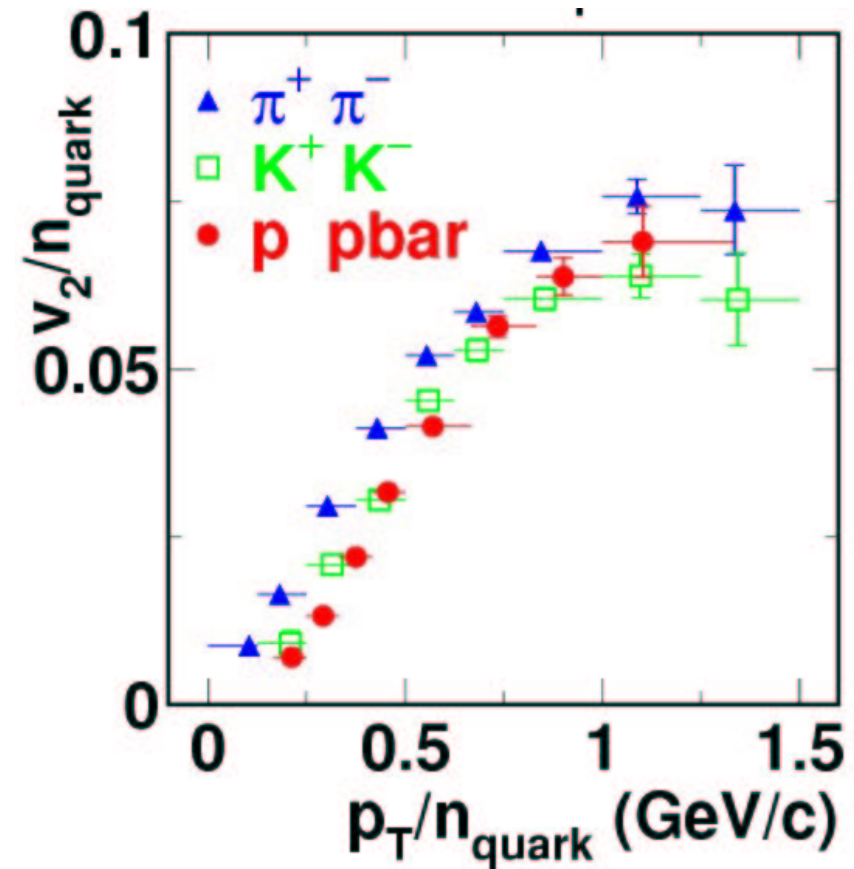
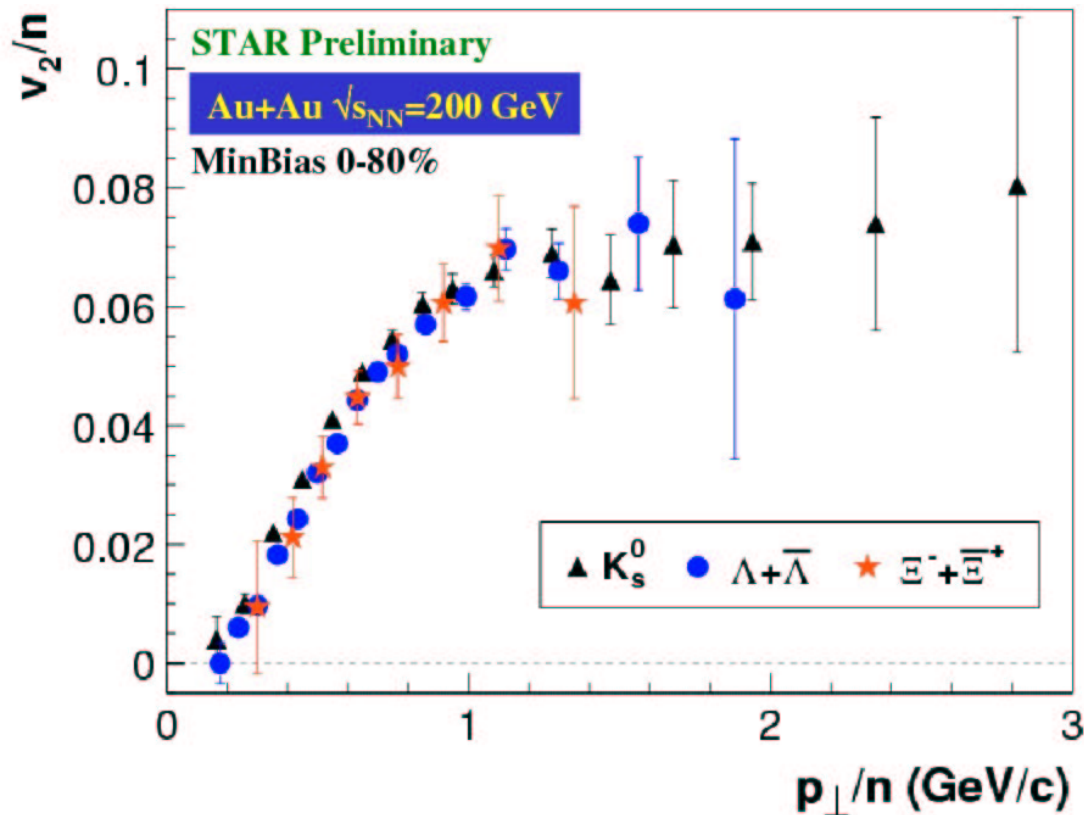
$\Rightarrow$  **factor 15 within reach**

# Success of flow scaling predictions

Sorensen [STAR], nucl-ex/0305008:  $K_0^S, \Lambda$

PHENIX, nucl-ex/0305013:  $\pi, K, p$

Castillo [STAR] at HIC03:  $\Xi$



- coalescence predictions confirmed for  $\pi, K, K_0, p, \Lambda, \Xi \rightarrow$  yet to see  $\Omega, \phi$
- interestingly, RHIC data indicate  $v_2^q \approx v_2^s$



# Story is not over...

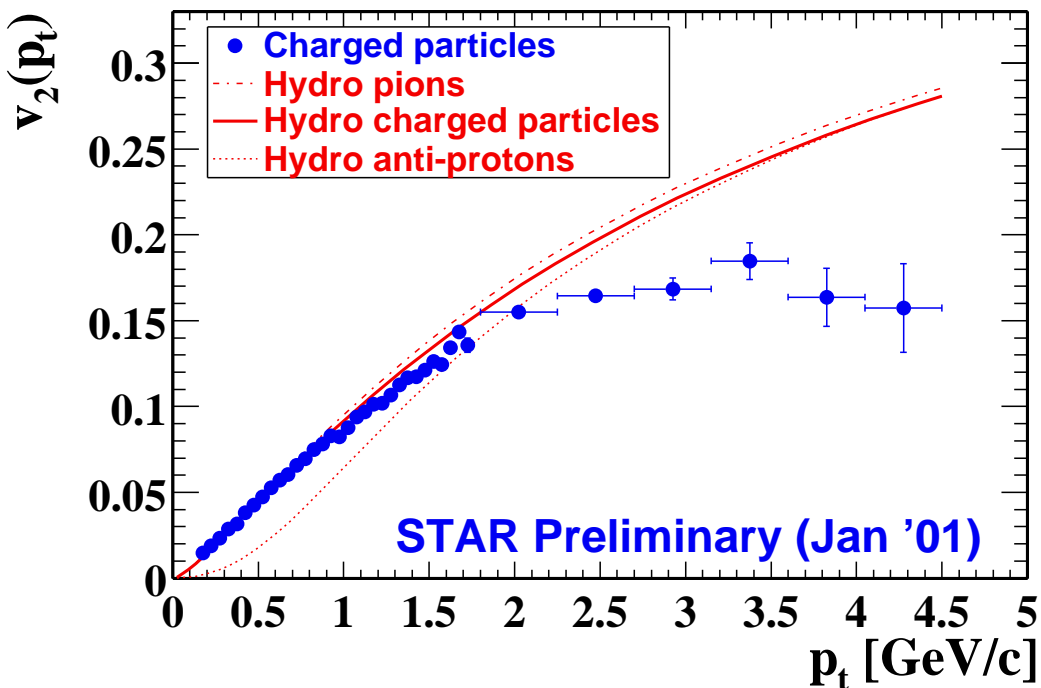
Further progress on all fronts possible/necessary

- **inelastic channels**
  - would love to see full 3+1D RHIC simulations one day
- **coalescence (hadronization)**
  - promising (also meson/baryon ratios) but treatment is oversimplified
  - check other observables
- **initial conditions?**
  - much better control desired
- **dynamics?**
  - critical scattering? strongly coupled regime?
  - correlation dominated limit ( $\chi$ )? - virtually unexplored
  - field/wave limit? 3+1D classical Yang-Mills?
  - **or maybe all is hydro?**

**Did the transport results prove hydro?**

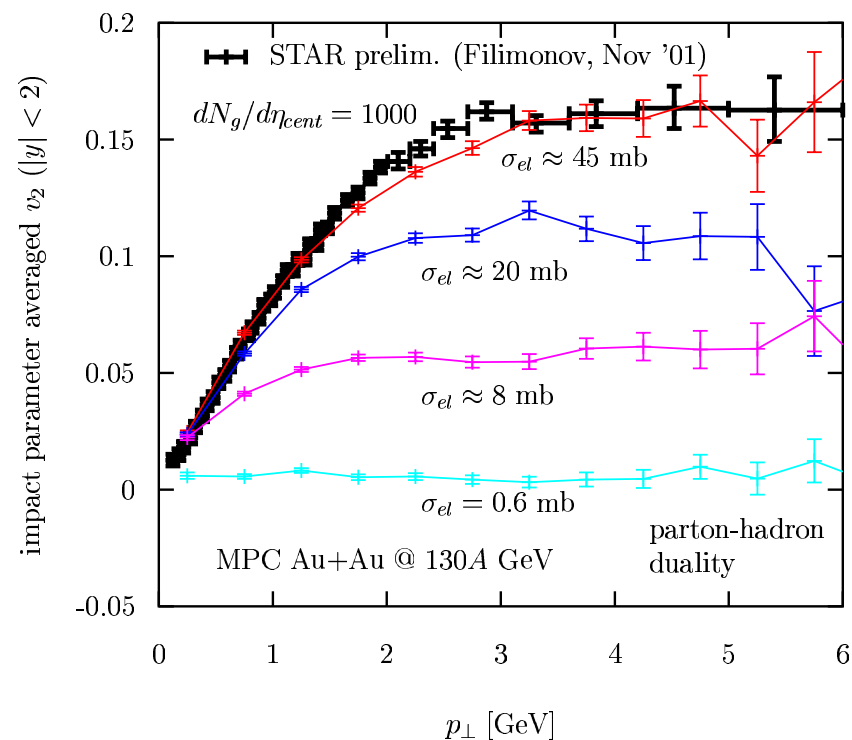
**Many think yes. BUT let's see...**

## ideal hydro (Kolb, Heinz, Snellings)



?

## transport



⇒ so, extreme 15x perturbative opacities justify hydro?

# Hydro

# Transport

“Infinite Opacity” Passage

?finite  $d\sigma$ ?  
?decoupling?

freezeout cond.  
initial cond.  
EOS  $e(p, n)$   
conservation laws

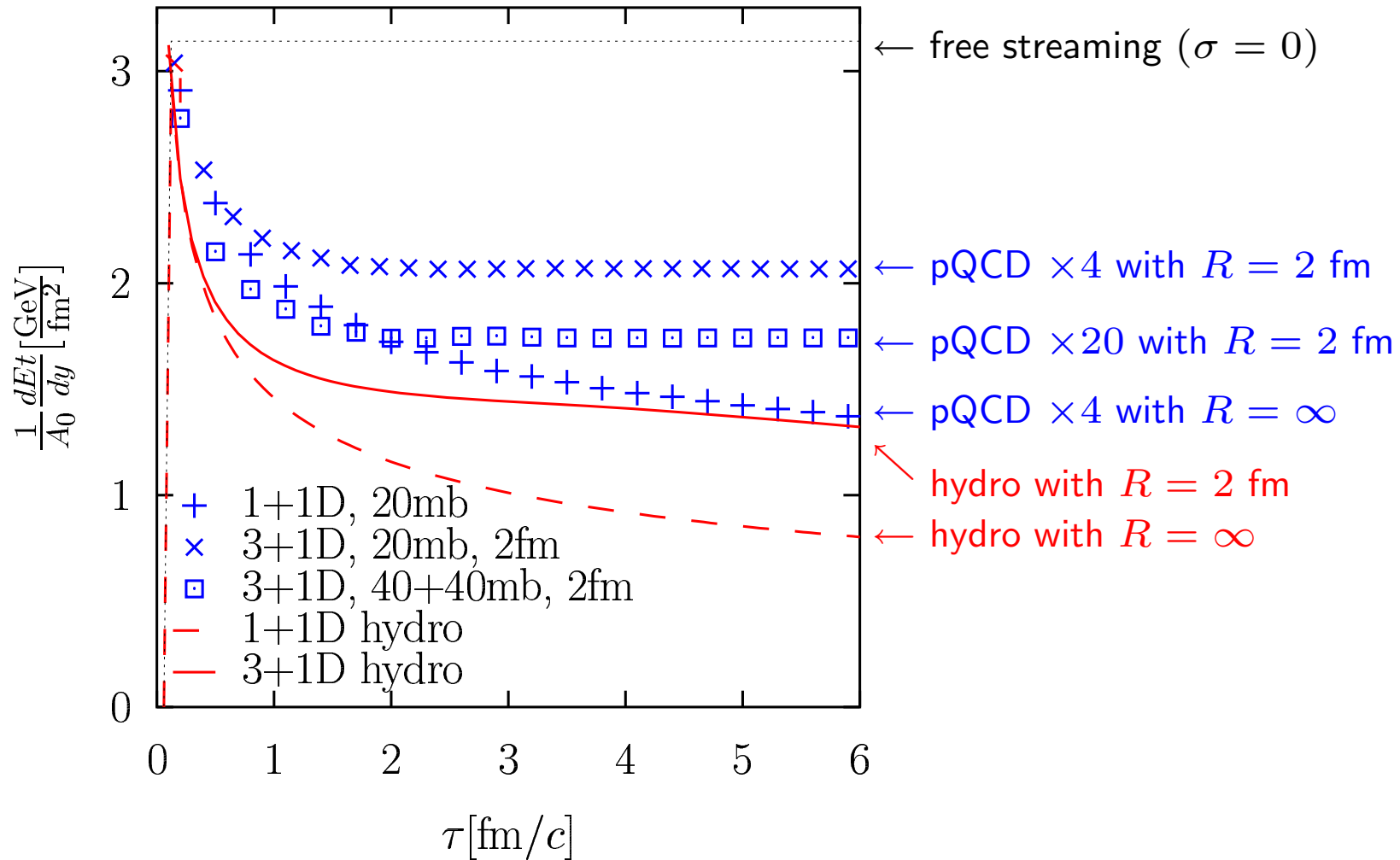
hadronization  
initial cond.  
 $d\sigma/dt$   
covariant BTE

12069 - ROPE BRIDGE OVER GORGE - A. J. ...

# One precursor: $E_T$ work

Gyulassy, Zhang, D.M.

MPC vs hydro (1+1D and 3+1D) PRC 62, 054907 ('00)



• **ideal hydro** (code: Rischke & Dumitru) **does more work** than transport

⇒ **even  $20\times$  pQCD opacities** found **insufficient** to maintain equilibrium

# How can both get the $v_2$ data then?

**Key: different initial conditions & thermodynamics**

## hydro:

- $\tau_0 = \tau_{th} = 0.6 \text{ fm}/c$
- QGP-in-bag + hadron gas EOS
- wounded nucleon entropy profile
- freezeout at  $T_{FO} \approx 120 \text{ MeV}$

## parton transport:

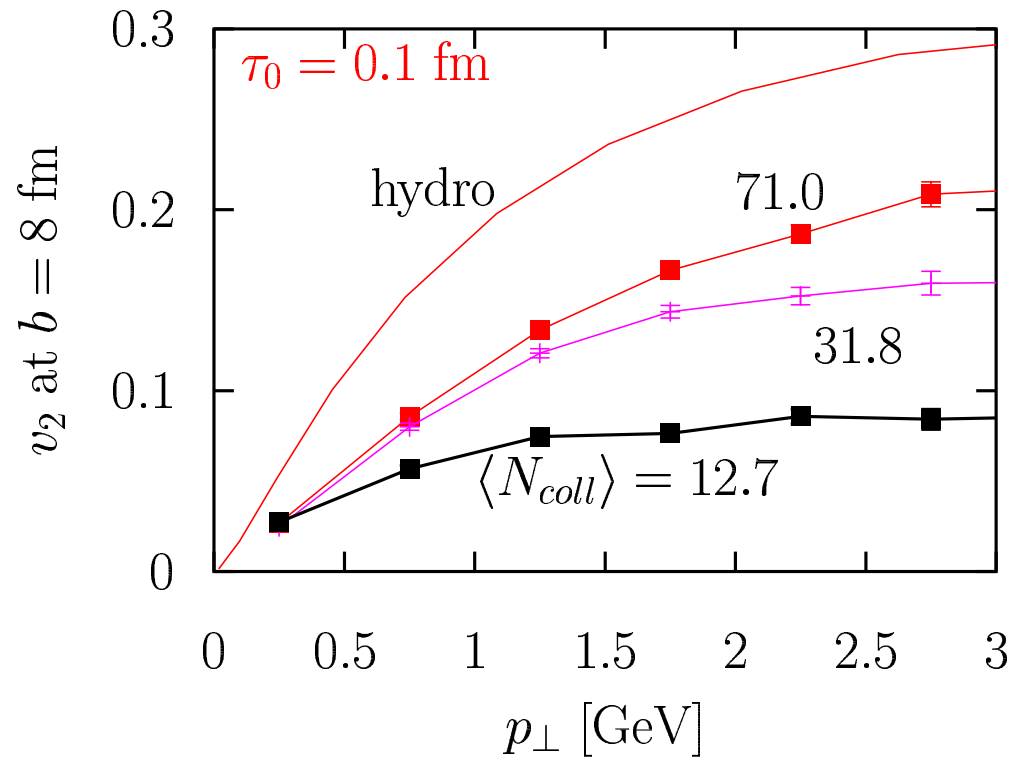
- $\tau_0 = \tau_{form} = 0.1 \text{ fm}/c$
- massless gas ( $e = 3p$ , if in thermal equil.)
- binary collision density profile

**$\Rightarrow$  apples to oranges comparison...**

# Apples-to-apples elliptic flow

Take same hydro and transport initconds & EOS, with  $\tau_0 = 0.1 \text{ fm}/c$   
( $T_0 = 700 \text{ MeV}$ , binary coll. profile,  $e = 3p$ ,  $b = 8 \text{ fm}$ ,  $dN/d\eta(b = 0) = 1000$ ,  $T_{FO} = 120 \text{ MeV}$ )

D.M. & Huovinen ('03):



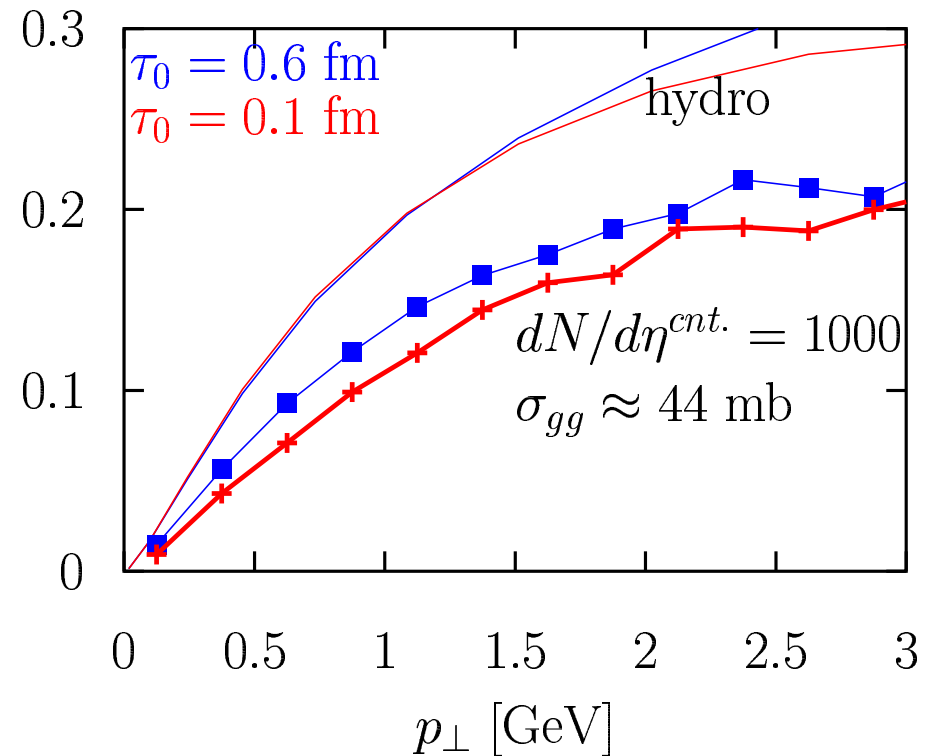
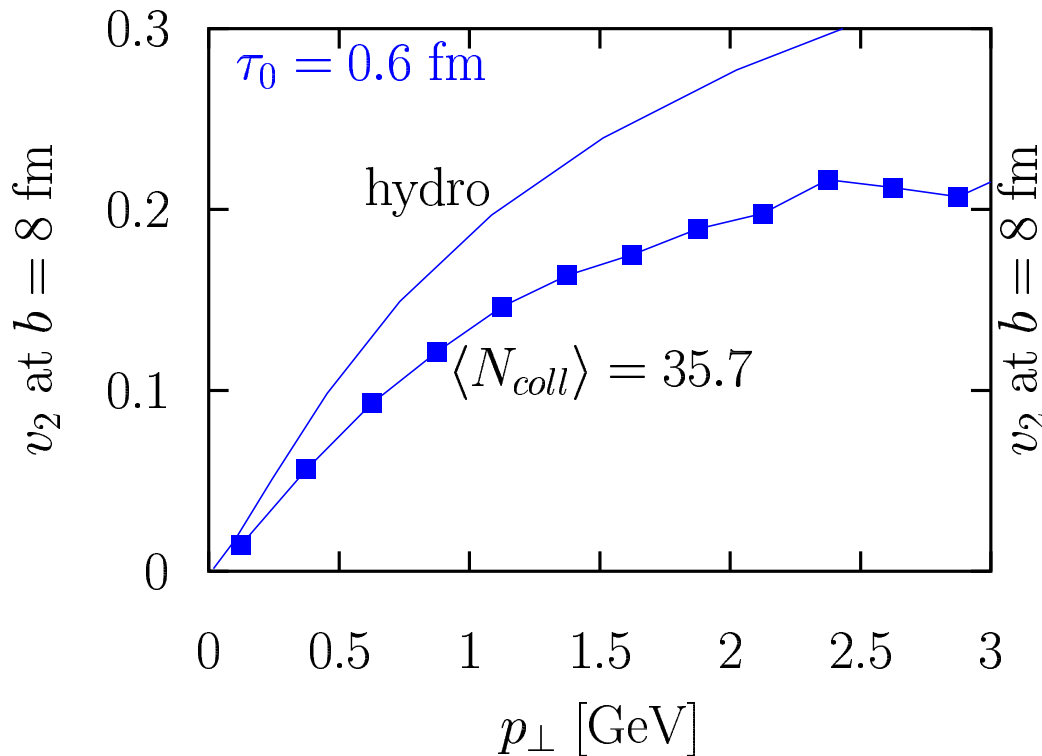
⇒ **large dissipation**, **transport  $v_2$  is 30-50% reduced** relative to hydro

→  $N_{coll} \gg 3$ , still not thermal - because of rapid longitudinal expansion

# Apples-to-apples elliptic flow (2)

Now same hydro and transport initconds but  $\tau_0 = 0.6 \text{ fm}/c$ , scaled  $T_0 \sim \tau_0^{-1/3}$

D.M. & Huovinen ('03):



⇒ **large dissipation**, transport  $v_2$  is 30-50% reduced relative to hydro

⇒ remarkably little sensitivity to initial time



# Extremely interesting

- **hydro:**

- remarkable **insensitivity** to initial time  $\rightarrow$  are QGP EOS results robust, too?
- is it an **accident**? or, can it be due to **common freezeout** temperature?
- any analytic understanding possible?

- **transport:**

- counter-intuitive: **fewer** collisions but same flow?

$$\langle n_{coll} \rangle = \int dt \frac{d\sigma_{el}}{dt} \int dz \rho \left( \vec{x}_0 + z\hat{n}, \tau = \frac{z}{c} \right) \approx \frac{dN}{dy} \frac{\sigma_{el}}{2\pi R_G^2} \log \frac{R_G}{\tau_0}$$

- on the other hand:

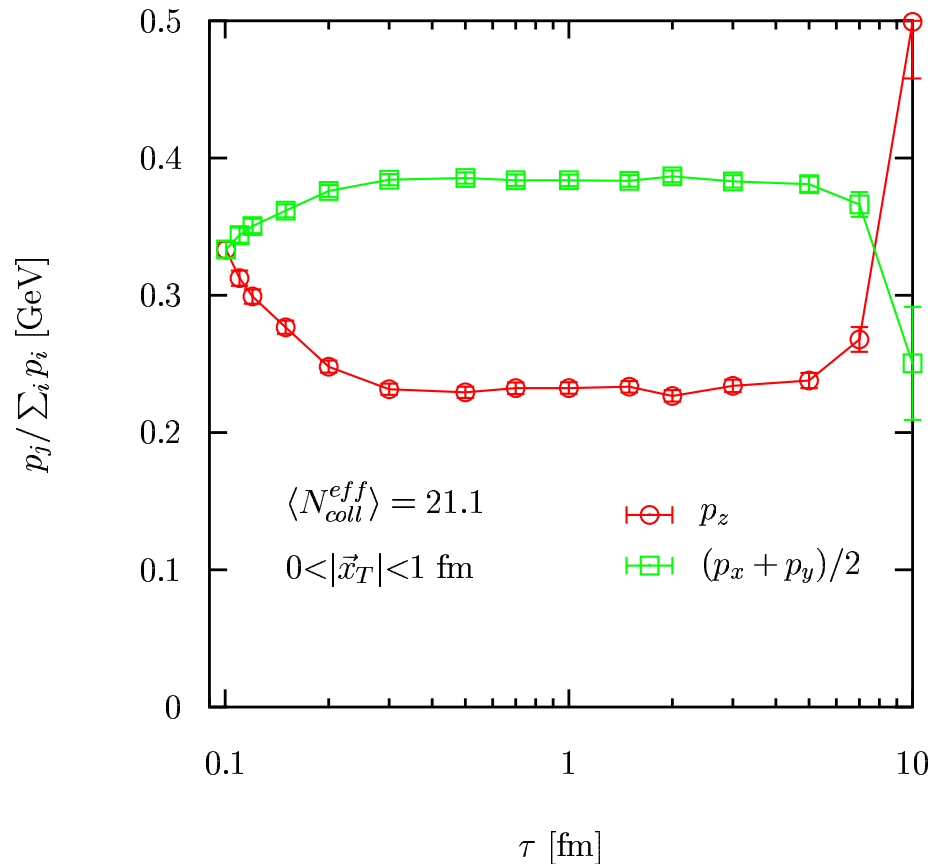
$$\Gamma_{coll} \propto n\sigma \propto 1/\tau, \quad \Gamma_{exp} \propto 1/\tau \quad \Rightarrow \quad \Gamma_{coll}/\Gamma_{exp} \sim const$$

- also only one scale [NPA 697, 495]  $R/\tau_0$  **changes**, while  $\sigma dN/d\eta$ ,  $\mu/T_0$  stay same

**In either case, 44 mb is insufficient for hydro limit  $\rightarrow$  need even larger.**

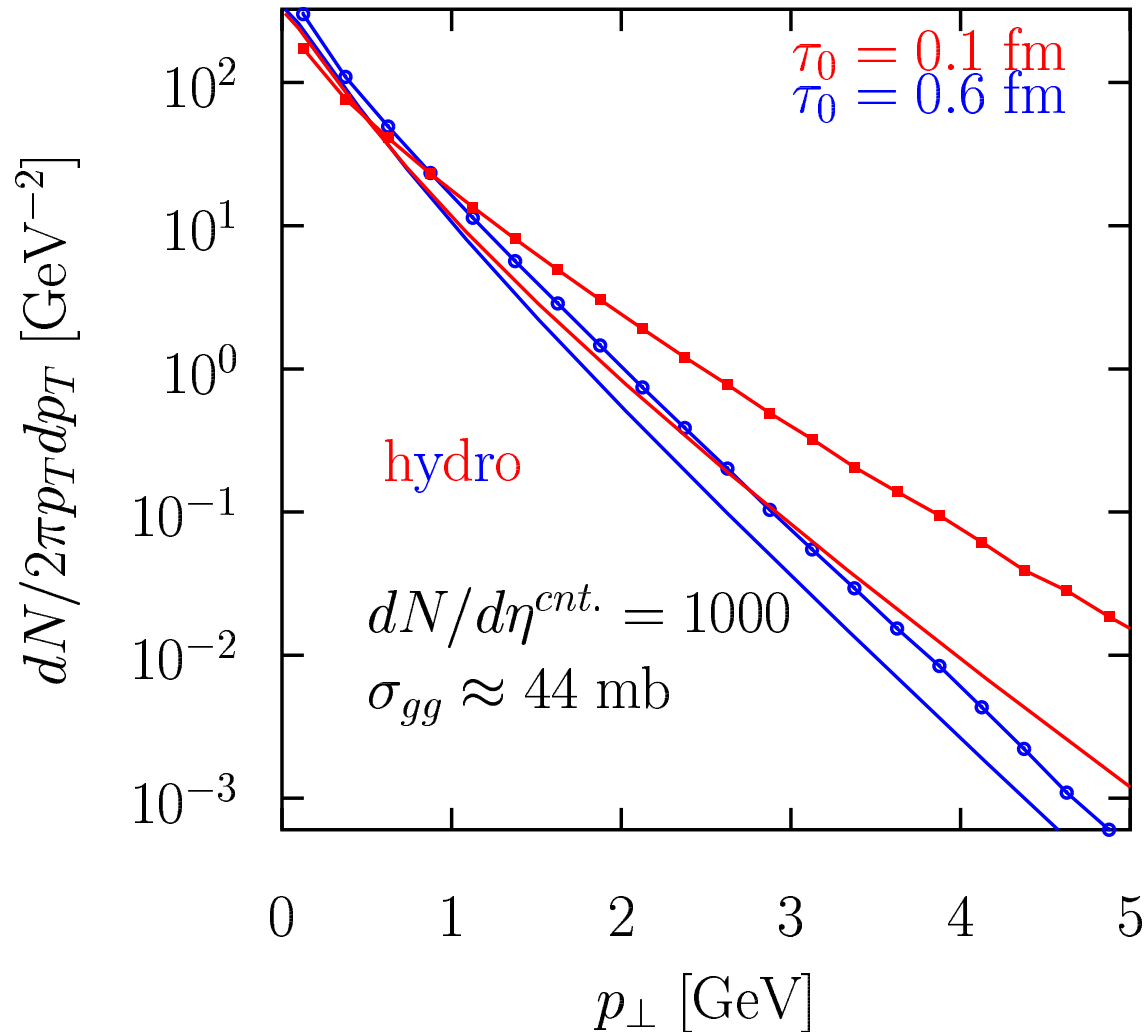
# Pressure anisotropy

Study pressure tensor  $b = 0$ ,  $\tau_0 = 0.1$  fm, (same minijet initial conditions)



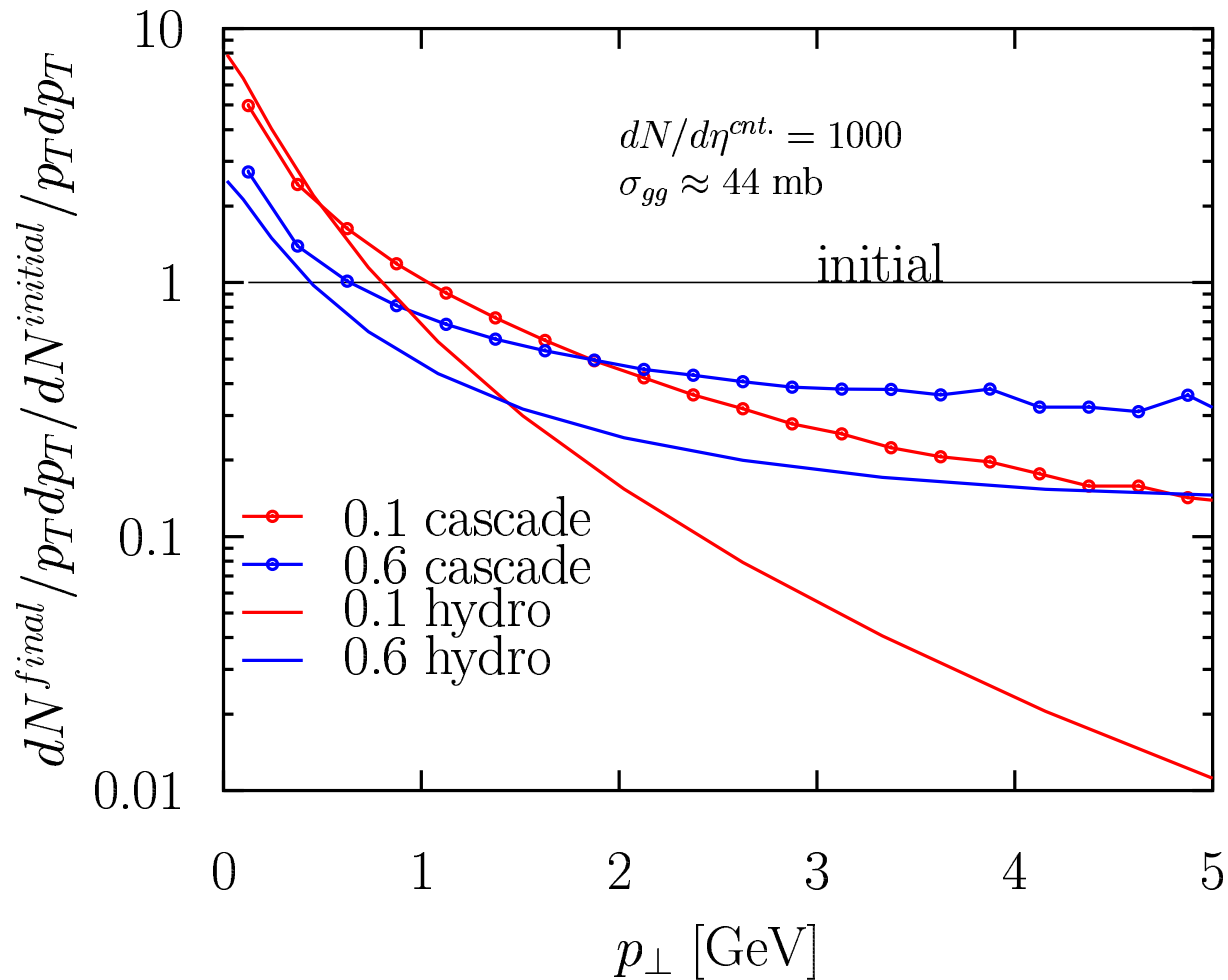
- even in center, **large pressure anisotropy**  $p_{trans} \sim 2p_z$
- evolution rapidly departs from hydro limit  $\rightarrow$  some anisotropic hydro?

# Final spectra



- transport spectra strongly depend on  $\tau_0 \rightarrow$  can one pinpoint form. time?
- hydro spectra are less sensitive, and agree below  $p_T < 1 \text{ GeV}$

# Quenching (final/initial)



• relative quenching weakens in transport for larger  $\tau_0$

⇒ maybe a larger  $\tau_0 > 1 \text{ fm}$  can save  $v_2$  vs quenching puzzle?

# Conclusions

- **What we learned:**

- large  $v_2$  at RHIC indicates **at least** pQCD opacities (and possibly much larger)
- absolutely amazing why hydro works - even **45mb is not enough**
- hydro and transport  $v_2$  seem robust against initial  $\tau_0$  (much less so for spectra)

- **Open issues (my incomplete list):**

- map out initial conditions - e.g., formation time?, initial condition models?
- better understanding of microscopic dynamics  
develop and test various dynamical models/limits, **make codes available** (OSCAR)  
**3+1D inelastic transport, viscous hydro, 3+1D ideal hydro, 3+1D Yang-Mills,**  
strongly coupled, highly-correlated systems, ...
- refine/further test hadronization models - e.g., parton coalescence
- $dE_T/dN(b) = const$  puzzle
- $v_2$  vs quenching puzzle
- high- $p_T$  angular correlations (flow vs jets)
- HBT puzzle