

(\* problem 2 \*)

ClearAll["Global`\*"]

(\* 1% salted water -

1 m<sup>3</sup> of water is 1000 kg, so 1% contains 10 kg salt by weight.

A NaCl molecule atomic weight is 23+

35.4 (noninteger because of mixture of isotopes) = \*)

In[1]:= mN = 1.68 \* 10<sup>-27</sup> \* kg

mNaCl = (23 + 35.4) \* mN

totalNaCl = 10 \* kg

nNaCl = totalNaCl / mNaCl / m<sup>3</sup>

10 000 / (23 + 35.4)

Out[1]= 1.68 × 10<sup>-27</sup> kg

Out[2]= 9.8112 × 10<sup>-26</sup> kg

Out[3]= 10 kg

Out[4]=  $\frac{1.01924 \times 10^{26}}{m^3}$

Out[5]= 171.233

kB = 1.38064852 × 10<sup>-23</sup> \* m<sup>2</sup> \* kg / s<sup>2</sup> / K;

(\* body temperature here \*)

T = (273 + 37) \* K

pNaCl = nNaCl \* kB \* T

310 K

$\frac{436\,237. \text{ kg}}{m \text{ s}^2}$

atm = 10<sup>5</sup> \* (kg \* m / s<sup>2</sup>) / m<sup>2</sup>

pNaCl / atm

$\frac{100\,000 \text{ kg}}{m \text{ s}^2}$

4.36237

(\* this is osmotic pressure in atm \*)

(\* problem 3, Otto cycle \*)

(\* points 1,2,3,4 have respective volumes, pressures and temperatures

Otto: 12 and 34 are adiabates,  $dQ=TdS=0$

23 and 41 are fixed volume,  $dW=pdV=0$

one needs to calculate efficiency using arbitrary  $C_v$ ,  $C_p$  and  $C_p/C_v=\gamma$

On fixed volume sides  $dU=$

$dQ$  so one can simply calculate efficiency from heat-in minus heat-out \*)

$$\eta = 1 - (C_v * (T_4 - T_1)) / (C_v * (T_3 - T_2))$$

$$V_2 = V_1 / r_1;$$

$$V_3 = V_2;$$

$$V_4 = V_1;$$

$$T_1 = p_1 * V_1 / R;$$

$$\text{Solve}[\{T_3 * V_3^{(\gamma + 1)} == T_4 * V_4^{(\gamma + 1)},$$

$$T_1 * V_1^{(\gamma + 1)} == T_2 * V_2^{(\gamma + 1)}, T_4 == T_1 * r_2\}, \{T_2, T_3, T_4\}]$$

$$1 - \frac{-T_1 + T_4}{-T_2 + T_3}$$

$$\left\{ \left\{ T_2 \rightarrow \frac{p_1 r_1 V_1^{1+\gamma} \left(\frac{V_1}{r_1}\right)^{-\gamma}}{R}, T_3 \rightarrow \frac{p_1 r_1 r_2 V_1^{1+\gamma} \left(\frac{V_1}{r_1}\right)^{-\gamma}}{R}, T_4 \rightarrow \frac{p_1 r_2 V_1}{R} \right\} \right\}$$

Assuming  $[V_1 > 0,$

$$\text{Simplify}[\eta /. \{T_2 \rightarrow \frac{p_1 r_1 V_1^{1+\gamma} \left(\frac{V_1}{r_1}\right)^{-\gamma}}{R}, T_3 \rightarrow \frac{p_1 r_1 r_2 V_1^{1+\gamma} \left(\frac{V_1}{r_1}\right)^{-\gamma}}{R}, T_4 \rightarrow \frac{p_1 r_2 V_1}{R}\}]]$$

$$1 - \left(\frac{1}{r_1}\right)^{1+\gamma}$$