

(* problem 1 electrons in Cu metal *)

ClearAll["Global`*"]

ne = 9 * 10²⁸ / m³;

ge = 2.;

kF = (6 * Pi² * ne / ge)^(1 / 3)

hbar = 6.626176 / (2 * Pi) * 10⁽⁻³⁴⁾ * kg * m² / s;

me = 9.1 * 10⁽⁻³¹⁾ * kg

EF = Assuming[m > 0, Simplify[(hbar² / 2 / me) * kF²]]

eV = 1.6 * 10⁽⁻¹⁹⁾ * kg * m² / s²;

EF / eV

$$1.3864 \times 10^{10} \left(\frac{1}{\text{m}^3} \right)^{1/3}$$

$$9.1 \times 10^{-31} \text{ kg}$$

$$\frac{1.17455 \times 10^{-18} \text{ kg m}^2}{\text{s}^2}$$

7.34092

(* problem 2 electrons in Cu metal, thermal correction
using (30.39) at fixed mu *)

kB = 1.38064852 * 10⁽⁻²³⁾ * m² * kg / s² / K;

T = 300 * K

delNoverN = Pi² / 8 * (kB * T / EF)²

300 K

0.0000153418

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(* problem 3a, nuclear matter as a Fermi gas *)
gN = 4;
nN = 0.16 * 10^ (45) / m^3;
kFN = ( 6 * Pi^2 * nN / gN) ^ (1 / 3)
mN = 1.67 * 10^ (-27) * kg;
EFN = Assuming[m > 0, Simplify[(hbar^2 / 2 / mN) * kFN^2]]
MeV = 10^6 * 1.6 * 10^ (-19) * kg * m^2 / s^2;
EFN / MeV
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$$1.33302 \times 10^{15} \left(\frac{1}{\text{m}^3} \right)^{1/3}$$

$$\frac{5.91689 \times 10^{-12} \text{ kg m}^2}{\text{s}^2}$$

36.9806

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(* problem 3b, neutron matter as a Fermi gas
only gN=2 is changed *)
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gN = 2;
kFN = ( 6 * Pi^2 * nN / gN) ^ (1 / 3)
EFN = Assuming[m > 0, Simplify[(hbar^2 / 2 / mN) * kFN^2]] / MeV
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$$1.6795 \times 10^{15} \left(\frac{1}{\text{m}^3} \right)^{1/3}$$

58.703

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(* the mean negative potential V should be such that V+36.9 MeV < 0,
but V+ 58.7 MeV > 0 *)
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(* problem 4 : thermal gas as a model for excited nucleus
here I express all in MeV *)
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ClearAll["Global`*"]
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In[72]:= (* ignoring one extra nucleon,
one conclude from (30.39) that  $\mu[T]=\mu[0]*(1+\text{Pi}^2/8*(\text{kB}*T/[0])^2)$ 
including it as done in (30.41) one finds that
delE=(5*Pi^2/12*(T/EFN)^2)*(3/5*A*EFN) *)
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```
In[73]:= A = 200;
DelEinMeV = 10;
EFNinMeV = 36.980581803094246`;
t = Solve[
  5 * Pi^2 / 12 * (TA / EFNinMeV)^2 * (3 / 5 * A * EFNinMeV) == DelEinMeV, TA][[2, 1, 2]];
t

$$\frac{t \cdot 10^6}{8.6173303 \times 10^{-5}}$$

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Out[77]= 0.865669

Out[78]= 1.00457×10^{10}

(* T is 0.865 MeV *)

```
In[88]:= A = 200;
kb = 1.38 * 10^-23;
n = 0.16 * 10^45;
m = 1.67 * 10^(-27);
h = 6.626176 / (2 * Pi) * 10^(-34);
DelE = 10 * 1.6021773 * 10^-13;
EFN = 36.980581803094246` * 1.6021773 * 10^-13;
EFNT[t_] := EFN * (1 - (Pi^2 * kb^2 * t^2) / (12 * EFN^2));
Solve[5 * Pi^2 / 12 * (kb * t / EFN)^2 * (3 / 5 * A * EFN) == DelE, t]
Solve[(2 * A / n) / (5 * Pi^2) * (2 * m / h^2)^3/2 * (EFNT[t]^5/2 + (5 * Pi^2 / 8) * (kb * t)^2 * EFNT[t]^1/2 - EFN^5/2) == DelE, t]
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Out[96]= {{t → -1.00504 × 10¹⁰}, {t → 1.00504 × 10¹⁰}}

Out[97]= {{t → -4.69011 × 10¹¹}, {t → -1.0041 × 10¹⁰},
 {t → 0. - 2.84749 × 10¹¹ i}, {t → 0. + 2.84749 × 10¹¹ i},
 {t → 0. - 1.08289 × 10¹² i}, {t → 0. + 1.08289 × 10¹² i}, {t → 0. - 1.0989 × 10¹² i},
 {t → 0. + 1.0989 × 10¹² i}, {t → 1.0041 × 10¹⁰}, {t → 4.69011 × 10¹¹}}