Electric dipole moment of the nucleon and light nuclei



A Tribute to Gerry Brown

Stony Brook | November 25, 2013 | Andreas Wirzba



Matter Excess in the Universe



1 End of inflation: $n_B = n_{\bar{B}}$

- 2 Cosmic Microwave Bkgr.
 - SM(s) prediction: (n_B-n_{B̄})/n_γ|_{CMB}~10⁻¹⁸
 - WMAP+COBE (2003): *n_B/n_γ*|_{CMB}=(6.1±0.3)10⁻¹⁰

Sakaharov conditions ('67) for dyn. generation of net *B*:

- 1 B violation to depart from initial B=0
- 2 C & CP violation

to distinguish B and \overline{B} production rates

3 non-equilibrium

to escape $\langle B \rangle = 0$ if CPT holds



The Electric Dipole Moment (EDM)



EDM: $\vec{d} = \sum_{i} \vec{r}_{i} e_{i} \xrightarrow{\text{subatomic}}_{\text{particles}} d \cdot \vec{S} / $ (polar) (axial)	ŝ
$\mathcal{H} = -\mu \frac{\vec{s}}{\vec{s}} \cdot \vec{B} - d\frac{\vec{s}}{\vec{s}} \cdot \vec{E}$ P: $\mathcal{H} = -\mu \frac{\vec{s}}{\vec{s}} \cdot \vec{B} + d\frac{\vec{s}}{\vec{s}} \cdot \vec{E}$ T: $\mathcal{H} = -\mu \frac{\vec{s}}{\vec{s}} \cdot \vec{B} + d\frac{\vec{s}}{\vec{s}} \cdot \vec{E}$	

Any non-vanishing EDM of some subatomic particle violates P&T

- Assuming CPT to hold, CP is violated as well
 → subatomic EDMs: "rear window" to CP violation in early universe
- Strongly suppressed in SM (CKM-matrix): $d_n \sim 10^{-31} e \text{ cm}$, $d_e \sim 10^{-38} e \text{ cm}$
- Current bounds: $d_n < 3 \cdot 10^{-26} e \text{ cm}$, $d_p < 8 \cdot 10^{-25} e \text{ cm}$, $d_e < 1 \cdot 10^{-28} e \text{ cm}$

n: Baker et al. (2006), p prediction: Dimitriev & Sen'kov (2003)*, e: Baron et al. (2013)[†]

* input from ¹⁹⁹Hg atom EDM measurement of Griffith et al. (2009) [†] from ThO molecule measurement Andreas Wirzba



A naive estimate of the scale of the nucleon EDM

Khriplovich & Lamoreaux (1997); Kolya Nikolaev (2012)

CP & P conserving magnetic moment ~ nuclear magneton μ_N

$$\mu_N=\frac{e}{2m_p}\sim 10^{-14}e\,\mathrm{cm}\,.$$

A nonzero EDM requires

parity P violation: the price to pay is $\sim 10^{-7}$

 $(G_F \cdot m_{\pi}^2 \sim 10^{-7} \text{ with } G_F \approx 1.166 \cdot 10^{-5} \text{GeV}^{-2})$,

and CP violation: the price to pay is ~ 10^{-3} $(|\eta_{+-}| \equiv |\mathcal{A}(\mathcal{K}_{L}^{0} \rightarrow \pi^{+}\pi^{-})| / |\mathcal{A}(\mathcal{K}_{S}^{0} \rightarrow \pi^{+}\pi^{-})| = (2.232 \pm 0.011) \cdot 10^{-3}).$

- In summary: $d_N \sim 10^{-7} \times 10^{-3} \times \mu_N \sim 10^{-24} e \,\mathrm{cm}$
- In SM (without θ term): extra $G_F m_{\pi}^2$ factor to undo flavor change

$$\Rightarrow d_N^{\rm SM} \sim 10^{-7} \times 10^{-24} e \, {\rm cm} \sim 10^{-31} e \, {\rm cm}$$

 \hookrightarrow The empirical window for search of physics BSM(θ =0) is

 $10^{-24}e\,\mathrm{cm} > d_N > 10^{-30}e\,\mathrm{cm}.$



Chronology of upper bounds on the neutron EDM



 \hookrightarrow 5 to 6 orders above SM predictions which are out of reach !



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Search for EDMs of charged particles in storage rings

General idea:



Initially longitudinally polarized particles interact with transversal \vec{E} \Rightarrow build-up of vertical polarization (measured with a polarimeter)

The spin precession relative to the momentum direction is given by the Thomas-BMT equation (for $\vec{\beta} \cdot \vec{B} = \vec{\beta} \cdot \vec{E} = 0$):

$$\frac{d\vec{S}^{*}}{dt} = \vec{\Omega} \times \vec{S}^{*} \quad \text{with} \quad \vec{\Omega} = -\frac{e}{m} \left(a\vec{B} + \left(\frac{1}{\gamma^{2} - 1} - a \right) \vec{\beta} \times \vec{E} + \eta (\vec{E} + \vec{\beta} \times \vec{B}) \right)$$
and
$$\vec{\mu} = (1 + a) \frac{e}{2m} \vec{S} / S \text{ and } \vec{d} = \eta \frac{e}{2m} \vec{S} / S$$



Method 1: pure electric ring

$$\vec{\Omega} = -\frac{e}{m} \left(\vec{A} \vec{B} + \underbrace{\left(\frac{1}{\gamma^{2-1}} - a\right) \vec{\beta} \times \vec{E}}_{:=0, \text{"Frozen spin method"}} + \eta(\vec{E} + \vec{\beta} \times \vec{B}) \right)$$

only possible for a > 0, *i.e.* for p and ³H, but not for d or ³He



Advantages:

١

- no magnetic field
- counter rotating beams

Disadvantage:

- not possible for deuterons ($a_D < 0$)

BNL or Fermilab?



Method 2: combined electric & magnetic ring

$$\vec{\Omega} = -\frac{e}{m} \left(\underbrace{a\vec{B} + \left(\frac{1}{\gamma^2 - 1} - a\right)\vec{\beta} \times \vec{E}}_{:=0, \text{"Frozen spin method"}} + \eta(\vec{E} + \vec{\beta} \times \vec{B}) \right)$$



Advantage:

- works for p, deuterons and ³He

Disadvantages:

- requires magnetic field
- two beam pipes
- magnetic coils made of copper

Jülich?



Method 3: pure magnetic ring





Advantage:

- existing COSY accelerator
- → precursor experiment:

First *direct* measurement of charged hadron EDMs

Disadvantage:

- lower sensitivity

JEDI@Jülich !



EDMs of the nucleon and especially light nuclei

$$\gamma_{n, D, {}^{3}\!He} \qquad \qquad \gamma_{n, D, {}^{3}\!He}$$

Outline:

- CP-violation beyond CKM matrix in the SM: $\mathcal{L}_{QCD} \theta$ -term (dim. 4)
 - EDM of the nucleon
 - EDM of the deuteron / EDM of helium-3
 - strategies of testing the $\bar{\theta}$ -term
- CP-violation from physics beyond the SM: SUSY, multi-Higgs,...
 - → dim. 6 sources: qEDM, qCEDM, gCEDM, 4qEDMs
 - EDM of the deuteron / EDM of helium-3
 - disentangling dim. 6 sources

Jülich-Bonn Collaboration (JBC):

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The $\mathcal{L}_{QCD} \theta$ -term in the SM

0

topologically non-trivial vacuum \rightarrow *GP* term in \mathcal{L}_{QCD} :

$$\mathcal{L} = \mathcal{L}_{\text{QCD}}^{\text{CP}} + \theta \frac{g_{S}^{2}}{32\pi^{2}} G_{\mu\nu}^{a} \tilde{G}^{a,\mu\nu}$$

$$\dots + \theta \frac{g_S^2}{32\pi^2} G_{\mu\nu}^a \tilde{G}^{a,\mu\nu} \xrightarrow{U_A(1)} \dots - \bar{\theta} m_q^* \sum_{f=u,d} \bar{q}_f i \gamma_5 q_f$$

with $\overline{\theta} = \theta + \arg \operatorname{Det} \mathcal{M}$, \mathcal{M} : quark mass matrix, $m_q^* \equiv \frac{m_u m_d}{m_u + m_d}$

$$d_n^{\bar{\theta}} \sim \bar{\theta} \cdot \frac{m_q^*}{\Lambda_{QCD}} \cdot \frac{e}{2m_n} \sim \bar{\theta} \cdot 10^{-2} \cdot 10^{-14} e \, \text{cm} \sim \bar{\theta} \cdot 10^{-16} e \, \text{cm} \quad \text{with} \ \bar{\theta} \stackrel{\text{NDA}}{\sim} \mathcal{O}(1).$$

 $d_n^{emp} < 2.9 \cdot 10^{-26} e \, \mathrm{cm} \rightsquigarrow |\bar{\theta}| < 10^{-10}$ strong CP problem



New Physics Beyond Standard Model (BSM)

SUSY, multi-Higgs, Left-Right-Symmetric models, ...

Effective field theory approach:

- All degrees of freedom beyond a specified scale are integrated out:
 → Only SM degrees of freedom remain: *q*, *g*, *H*, *W*[±],...
- Relics of eliminated BSM physics 'remembered' by the values of the low-energy constants (LECs) of the CP-violating contact terms, e.g.





SM plus all possible T- and P-odd contact interactions

Removal of Higgs and W^{\pm} bosons & transition to hadronic fields (plus mixing):

Order the interactions by power counting





Road map from EDM Measurements to EDM Sources

Experimentalist's point of view \rightarrow

← Theorist's point of view



(adapted from Jordy de Vries, Jülich, March 14, 2013)



EDM Translator from 'quarkish/machine' to 'hadronic/human' language?



Symmetries (esp. chiral one) and Goldstone Theorem Low-Energy Effective Field Theory with External Sources *i.e.* Chiral Perturbation Theory (suitably extended)

Andreas Wirzba

 \rightarrow



θ -Term on the Hadronic Level

hadronic level: non perturbative techniques required: e.g. 2-flavor ChPT

Symmetries of QCD preserved by the effective field theory (EFT)



Lebedev et al. (2004), Mereghetti et al. (2010), Bsaisou et al. (2013)



θ-Term Induced Nucleon EDM

single nucleon EDM:



"controlled"



$$d_n|_{\text{loop}}^{\text{isovector}} = e \frac{g_{\pi NN} g_0^{\phi}}{4\pi^2} \frac{\ln(M_N^2/m_{\pi}^2)}{2M_N} \sim \bar{\theta} m_{\pi}^2$$

Crewther, di Vecchia, Veneziano & Witten (1979); Pich & de Rafael (1991); Ottnad et al. (2010)

$$g_0^{\theta} = \frac{(m_n - m_p)^{\text{strong}} (1 - \epsilon^2)}{4F_{\pi}\epsilon} \bar{\theta} \approx (-0.018 \pm 0.007) \bar{\theta} \quad (\text{where } \epsilon \equiv \frac{m_u - m_d}{m_u + m_d})$$

 $\hookrightarrow d_n |_{loop}^{isovector} \sim -(2.1 \pm 0.9) \cdot 10^{-16} \,\overline{\theta} \, \mathrm{e\, cm} \qquad \text{Ottnad et al. (2010); Bsaisou et al. (2013)}$

But what about the two "unknown" coefficients of the contact terms?



We'll always have ... the lattice

However, It's a long way to Tipperary ...



θ = 1 (adapted from Eigo Shintani (Mainz & RBRC), *MITP Workshop*, *Mainz*, *Oct.* 10, 2013)

Don't mention the ... light nuclei



θ-Term Induced Nucleon EDM:

Crewther, di Vecchia, Veneziano & Witten (1979); Pich & de Rafael (1991); Ottnad et al. (2010)

single nucleon EDM:





θ-Term Induced Nucleon EDM:

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single nucleon EDM:





EDM of the Deuteron at LO: quantitative θ -term results



in units of $g_1^{\theta} e \cdot fm \cdot (g_A m_N / F_{\pi})$

Ref. potential no ³ P ₁ -int v		with ³ P ₁ -int	total	
JBC (2013)*	A <i>v</i> 18	-1.93×10^{-2}	$+0.48 \times 10^{-2}$	-1.45×10^{-2}
JBC (2013)	CD Bonn	-1.95×10^{-2}	$+0.51 \times 10^{-2}$	-1.45×10^{-2}
JBC (2013)*	ChPT (N ² LO) [†]	-1.94×10^{-2}	$+0.65 \times 10^{-2}$	-1.29×10^{-2}
Song (2013)	A <i>v</i> 18	-	-	-1.45×10^{-2}
Liu (2004)	A <i>v</i> ₁₈	-	-	-1.43×10^{-2}
Afnan (2010)	Reid 93	-1.93×10^{-2}	$+0.40 \times 10^{-2}$	-1.43×10^{-2}

*: in preparation [†]: cutoffs at 600 MeV (LS) and 700 MeV (SFR)

BSM GP sources: LO $g_1 \pi NN$ -vertex also exists in qCEDM and 4qLR cases



³He EDM: quantitative results for g₀ exchange



 $g_0 N^{\dagger} \vec{\pi} \cdot \vec{\tau} N$ (*CP*, I) θ -term, qCEDM \rightarrow LO 4qLR \rightarrow N²LO

units: $g_0(g_A m_N/F_{\pi})e$ fm

author	potential	no int.	with int.	total
JBC (2013)*	Av ₁₈ UIX	-0.45×10^{-2}	-0.13×10^{-2}	-0.57×10^{-2}
JBC (2013)*	CD BONN TM	-0.56×10^{-2}	-0.12×10^{-2}	-0.67×10^{-2}
JBC (2013)*	ChPT (<i>N²LO</i>) [†]	-0.56×10^{-2}	-0.19×10^{-2}	-0.76×10^{-2}
Song (2013)	Av ₁₈ UIX	-	-	-0.59×10^{-2}
Stetcu (2008)	Av ₁₈ UIX	-	-	-1.21×10^{-2}

*: in preparation [†]: cutoffs at 600 MeV (LS) and 700 MeV (SFR)

Results for ${}^{3}H$ also available (not shown)

Note: calculation finally under control !



³He EDM: quantitative results for g₁ exchange



 $\begin{array}{ll} g_1 N^{\dagger} \pi_3 N & (CP, \cline I) \\ \theta \mbox{-term} & \rightarrow & \mbox{NLO} \\ qCEDM, \mbox{4qLR} & \rightarrow & \mbox{LO} \end{tabular} \end{array}$

units: $g_1(g_A m_N/F_{\pi})e$ fm Ref. potential no int. with int. total -0.02×10^{-2} -1.09×10^{-2} -1.11×10^{-2} JBC (2013)* Av18UIX CD BONN TM -1.11×10^{-2} -0.03×10^{-2} -1.14×10^{-2} JBC(2013)* -1.09×10^{-2} -0.14×10^{-2} -0.96×10^{-2} JBC (2013)* ChPT (N²LO)[†] Song (2013) Av18UIX -1.08×10^{-2} -2.20×10^{-2} Stetcu (2008) AV18 UIX --

*: in preparation [†]: cutoffs at 600 MeV (LS) and 700 MeV (SFR) Results for ³H also available (not shown)

In the pipeline: \mathcal{QP} 3π -vertex contribution (4qLR: LO)



Quantitative EDM results in the θ -term scenario

Single Nucleon (with adjusted signs for consistency; note here e < 0):

$$-d_{1}^{\text{loop}} \equiv \frac{1}{2}(d_{n} - d_{p})^{\text{loop}}$$

= $(2.1 \pm 0.9) \cdot 10^{-16} \,\overline{\theta} \, e \, \text{cm}$ (Bsaisou et al. (2013))
$$d_{n} = +(2.9 \pm 0.9) \cdot 10^{-16} \,\overline{\theta} \, e \, \text{cm}$$
 (Guo & Meißner (2012))
$$d_{p} = -(1.1 \pm 1.1) \cdot 0^{-16} \,\overline{\theta} \, e \, \text{cm}$$
 (Guo & Meißner (2012))

Deuteron:

$$d_D = d_n + d_p - \left[(0.59 \pm 0.39) - (0.05 \pm 0.02) \right] \cdot 10^{-16} \,\overline{\theta} \, e \, \text{cm}$$

= $d_n + d_p - (0.54 \pm 0.39) \cdot 10^{-16} \,\overline{\theta} \, e \, \text{cm}$ (Bsaisou et al. (2013))

Helium-3:

$$d_{^{3}He} = \tilde{d}_{n} + \left[(1.52 \pm 0.60) - (0.46 \pm 0.30) \right] \cdot 10^{-16} \,\bar{\theta} \,e\,\text{cm}$$

= $\tilde{d}_{n} + (1.06 \pm 0.67) \cdot 10^{-16} \,\bar{\theta} \,e\,\text{cm}$ (JBC (2013))
with $\tilde{d}_{n} = 0.88d_{n} - 0.047d_{p}$ (de Vries et al. (2011))



Testing Strategies in the θ EDM scenario

Remember:

d_D	=	$d_n + d_p$	$-(0.54 \pm 0.39) \cdot 10^{-16} ar{ heta} e { m cm}$	(Bsaisou et al. (2013))
d₃ _{He}	=	\widetilde{d}_n	+ $(1.06 \pm 0.67) \cdot 10^{-16} \overline{\theta} e \mathrm{cm}$	(JBC (2013))

Testing strategies:

- plan A: measure d_n , d_p , and $d_D \xrightarrow{d_D(2N)} \overline{\theta} \xrightarrow{\text{test}} d_{^3He}$
- plan A': measure d_n , (d_p) , and $d_{^{3}He} \xrightarrow{d_{^{3}He}(2N)} \overline{\theta} \xrightarrow{\text{test}} d_D$
- plan B: measure d_n (or d_p) + Lattice QCD $\sim \bar{\theta} \xrightarrow{\text{test}} d_D$
- plan B': measure d_n (or d_p) + Lattice QCD $\rightsquigarrow \overline{\theta} \xrightarrow{\text{test}} d_p$ (or d_n)













here: only absolute values considered





here: only absolute values considered



Conclusions

- (Hadronic) EDMs play a key role in probing new sources of GP
- Measurements of hadronic EDMs are low-energy measurements
 → Predictions have to be given in the *empirical language of hadrons* → only reliable methods predicting *uncertainties* as well: *ChPT/EFT* and/(or ultimately) *Lattice QCD*
- EDMs of light nuclei provide independent information to nucleon EDMs and may be even larger and even simpler
- Deuteron and helium-3 nuclei serve as isospin filters for EDMs

At least the EDMs of *p*, *n*, *d*, and ³He have to be measured to disentangle the underlying physics by applying methods of EFT and lattice QCD



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