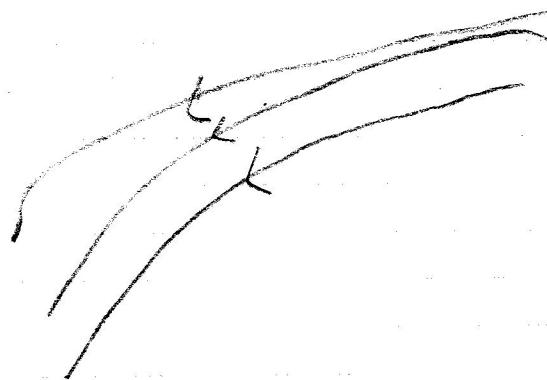
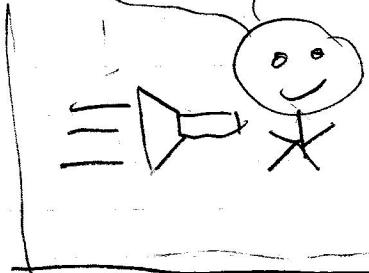


I'm watching
you fall into sun
• and your
light is bending



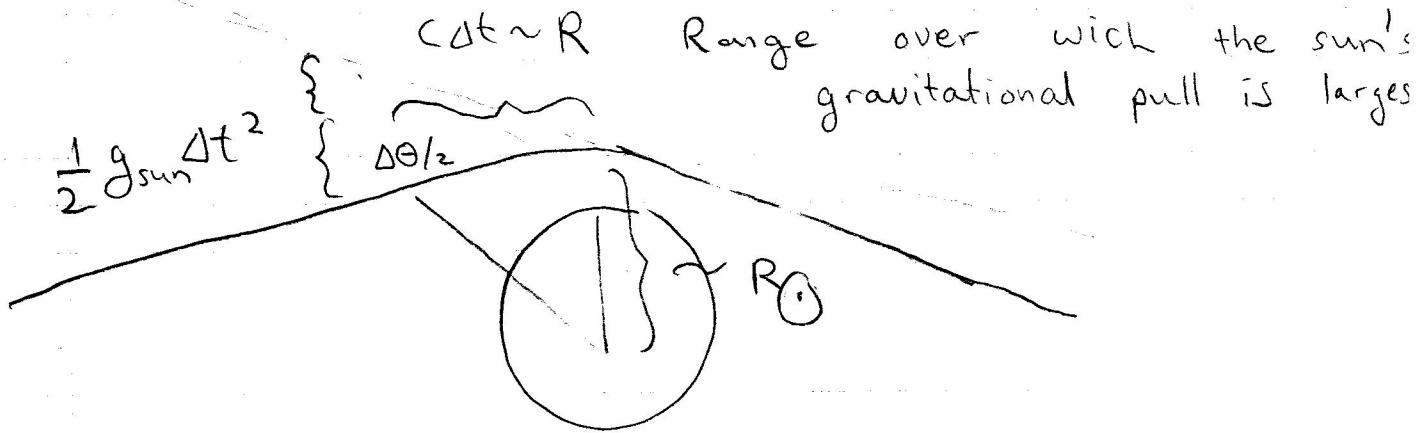
Who says
I'm falling
I feel no forces
and light moves straight
according to me



$$\Delta y \sim \frac{1}{2} g t^2$$

↙ Sun
Center

Estimate:



Now use:

$$\textcircled{1} \quad g_{\text{sun}}(R) \sim \frac{GM_0}{R^2}$$

- $\textcircled{2}$ The time over which the sun's gravity bends the light is

$$c\Delta t \sim R$$

When $c\Delta t$ is much larger than R
the gravity is weak

- $\textcircled{3}$ $R \sim R_{\odot}$, our light rays skim the sun

So

So

$$\frac{\Theta}{2} \sim \frac{1}{2} \frac{g_{\text{sun}}(R) \Delta t^2}{c \rho t}$$

$$\Theta \sim \frac{G M_0}{c R^2} \cdot \frac{R}{c}$$

$$\Theta \sim \frac{G M_0}{c^2 R}$$

Taking

$$G = 6.67 \times 10^{-11} \text{ m}^3/\text{kg s}^2$$

$$M_0 = 2 \times 10^{30} \text{ kg}$$

$$R_0 = 700,000 \text{ km}$$

So

$$\Theta \sim 0.43'' \text{ arcsec}$$

A proper General Relativistic treatment gives

$$\Theta \approx 1.75 \text{ arcsec}$$

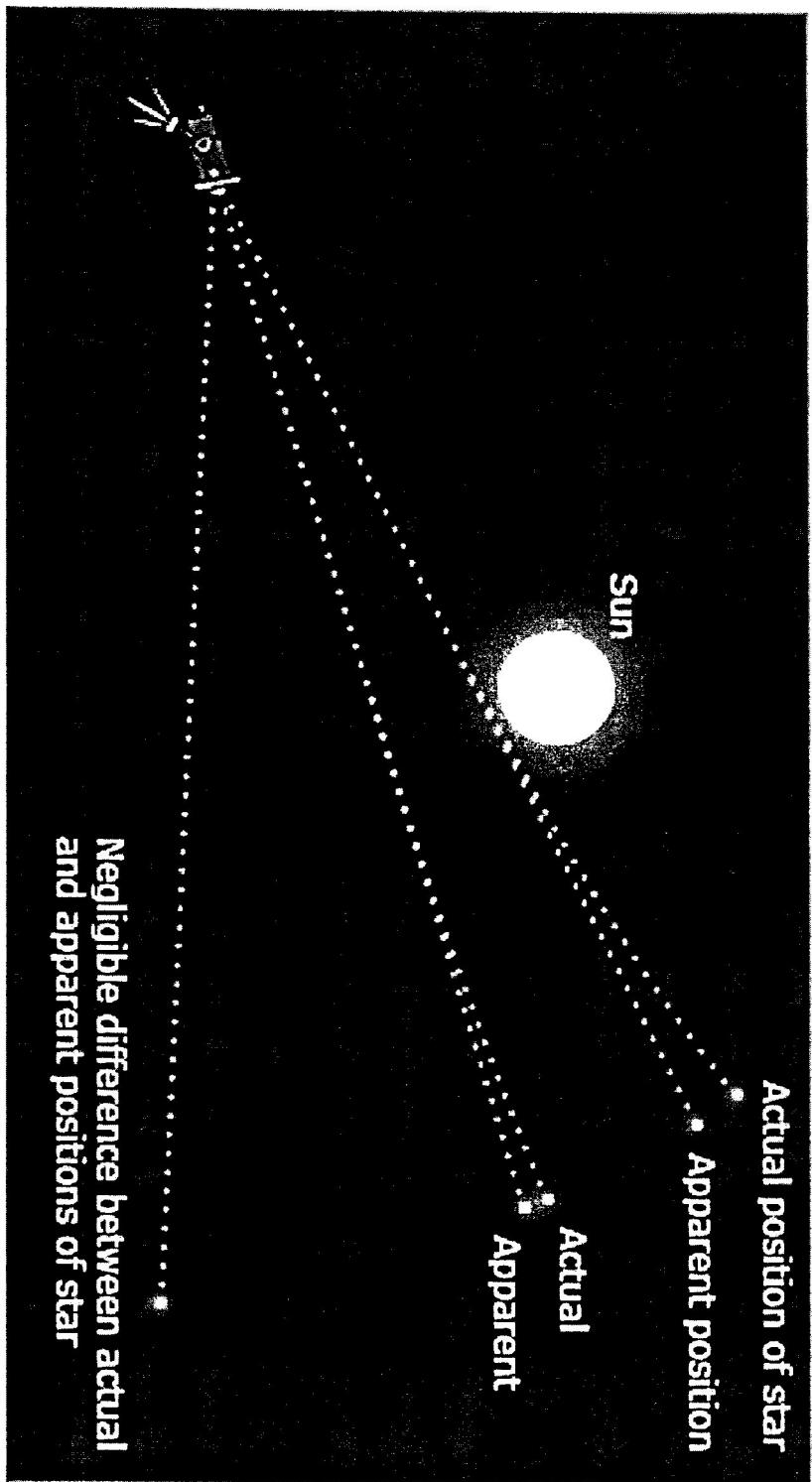
Incidentally Einstein originally predicted

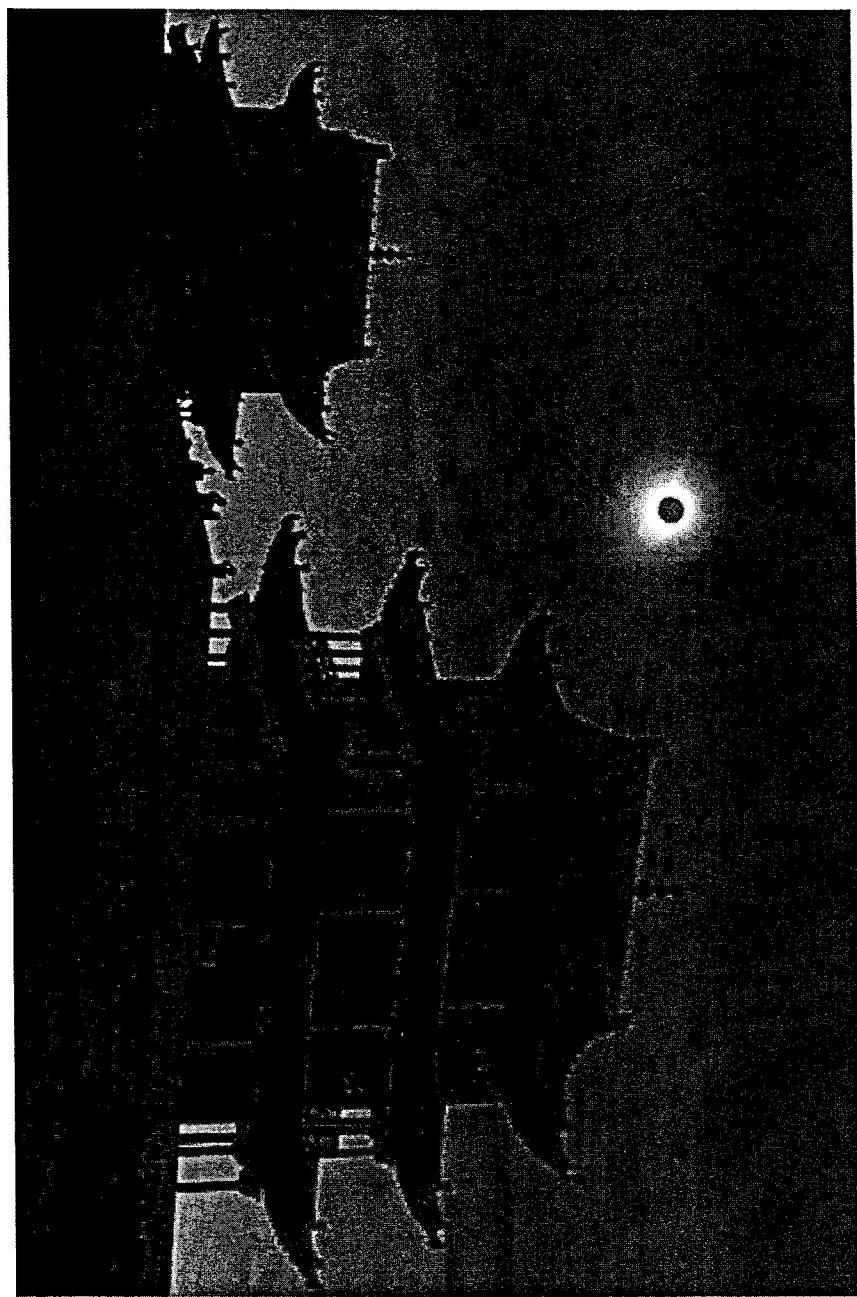
$$\Theta \approx 0.87 \text{ arcsec} \quad \text{well}$$

But corrected the result later (^vBefore
the experiment in 1919)

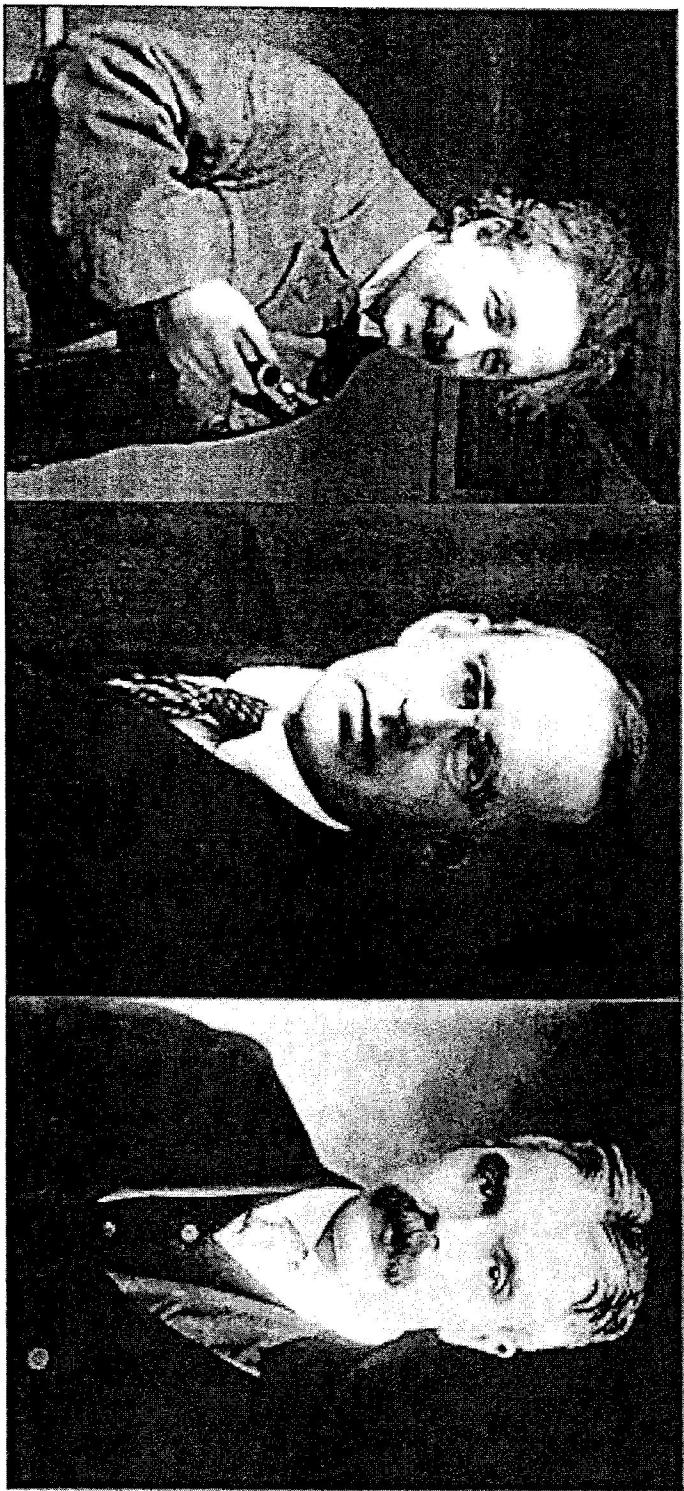
Measuring the bending of light

- Measure the deflection of starlight as it goes near the sun
- Compare angles between the stars during a solar eclipse, and at night at a different time of the year



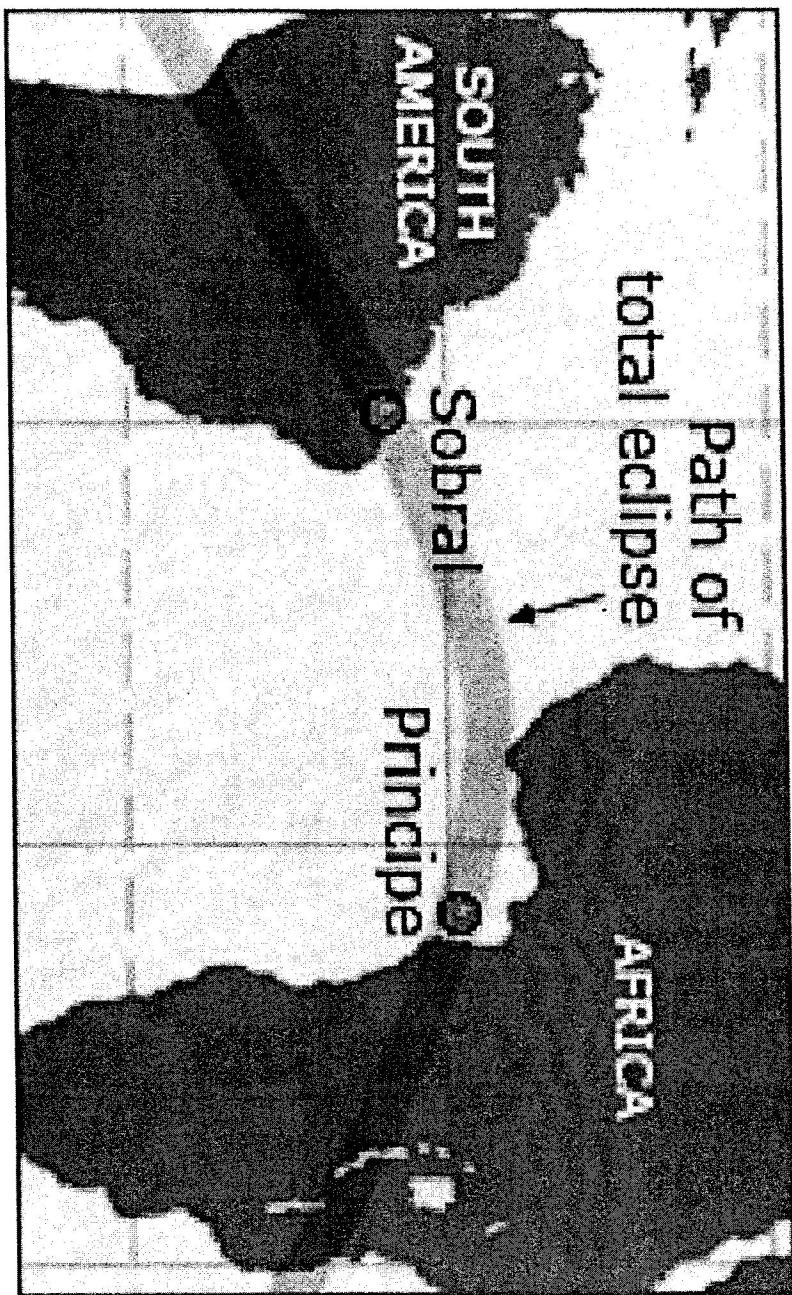


The men of the 1919 measurement – Einstein, Eddington, Dyson



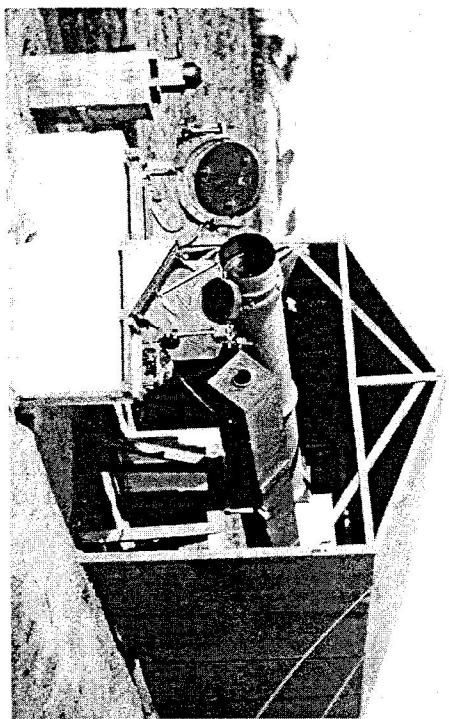
source http://undsci.berkeley.edu/article/0_0_0/fair_tests_04

Eddington and Dyson travel to the tropics at Sorbal and Principe

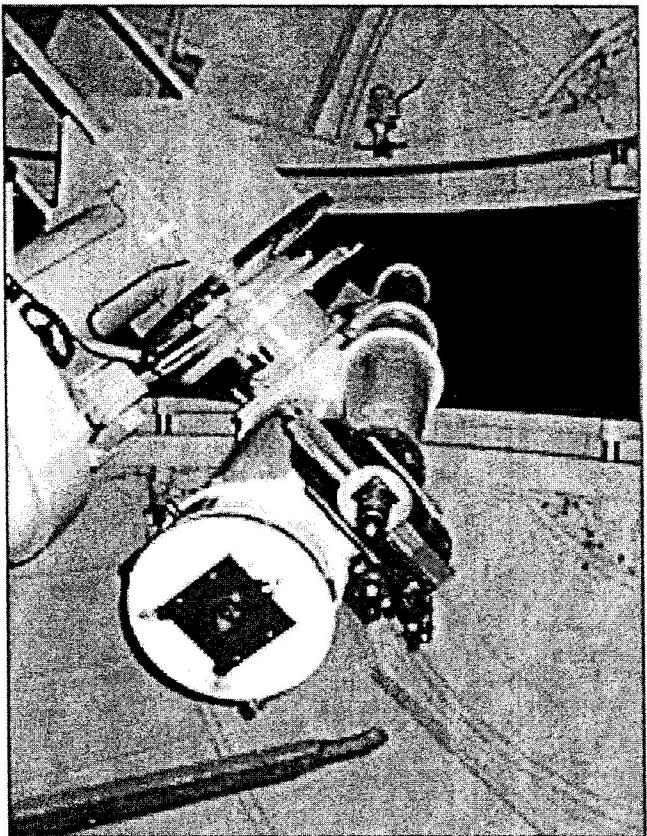


source http://undsci.berkeley.edu/article/0_0_0/fair_tests_04

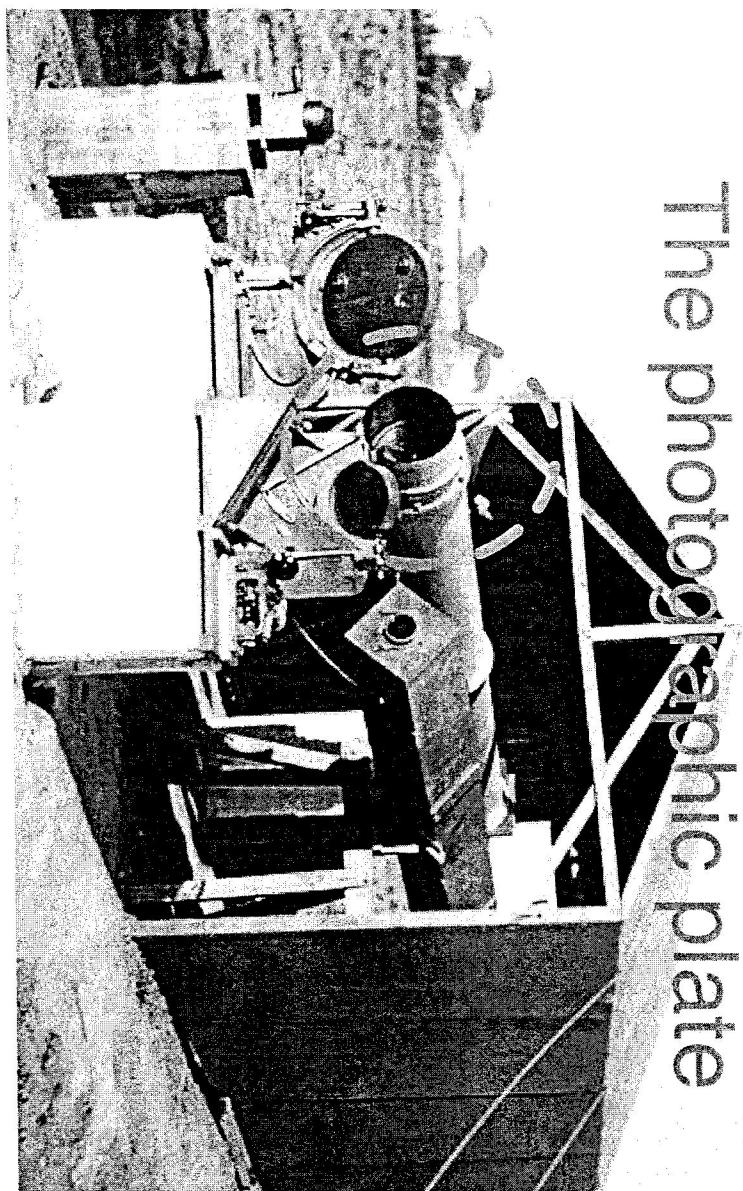
... And set up telescopes in the Tropics and at Cambridge



Instruments at Sobral, Brazil.
The 4-inch lens is in the square tube on the right, and the astrographic lens, chosen for its wide field of view, is in the circular tube on the left. In front of the tubes are mirrors that are driven by a mechanism that keeps the stellar images at the same position on the plates during an exposure. The mirror on the left was the chief suspect in the poor-quality astrophotographic-lens images produced during the 1919 eclipse.
(Courtesy of the Science Museum, London.)



Record image on plate

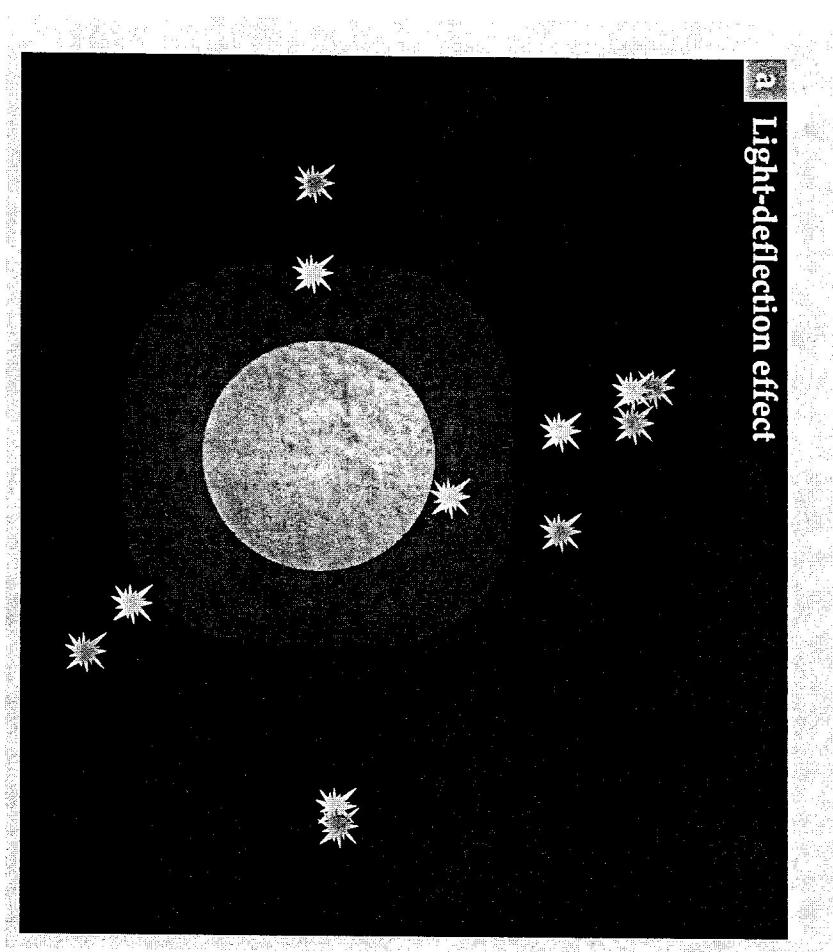


The photographic plate

Instruments at Sobral, Brazil.

The 4-inch lens is in the square tube on the right, and the astrophotographic lens, chosen for its wide field of view, is in the circular tube on the left. In front of the tubes are mirrors that are driven by a mechanism that keeps the stellar images at the same position on the plates during an exposure. The mirror on the left was the chief suspect in the poor-quality astrophotographic-lens images produced during the 1919 eclipse. (Courtesy of the Science Museum, London.)

. . . And finally measure the deflection by reading the positions between the stars off of photographic plates with a micrometer and comparing to other plates

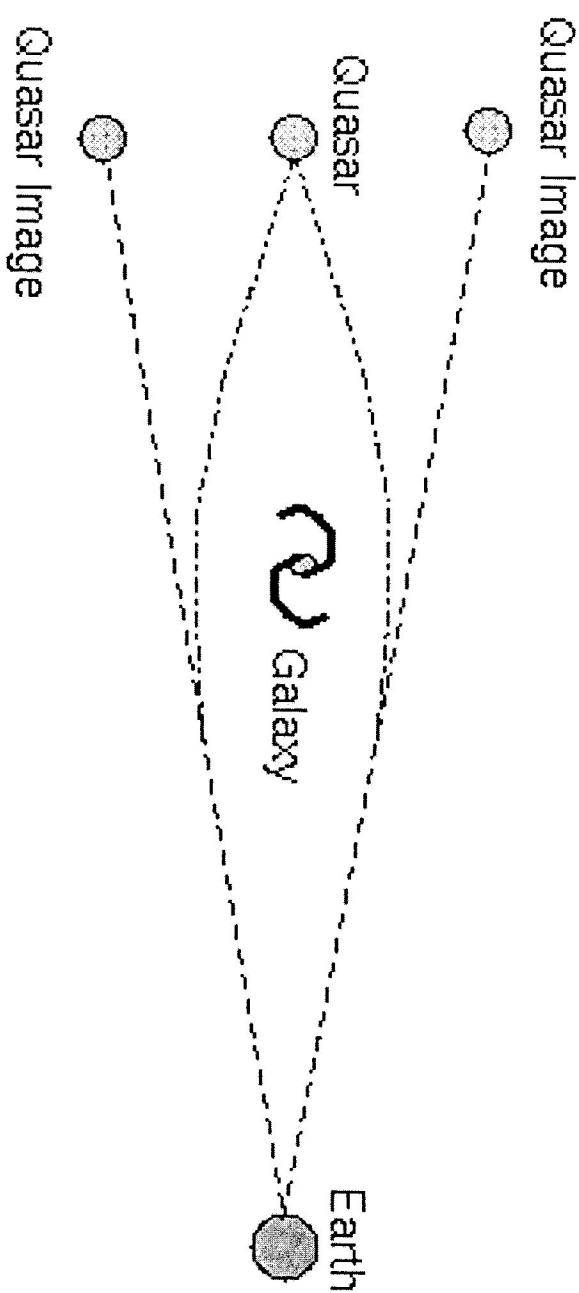


a Light-deflection effect

The experimental result agrees with Einstein's prediction of 1.7 arcsec

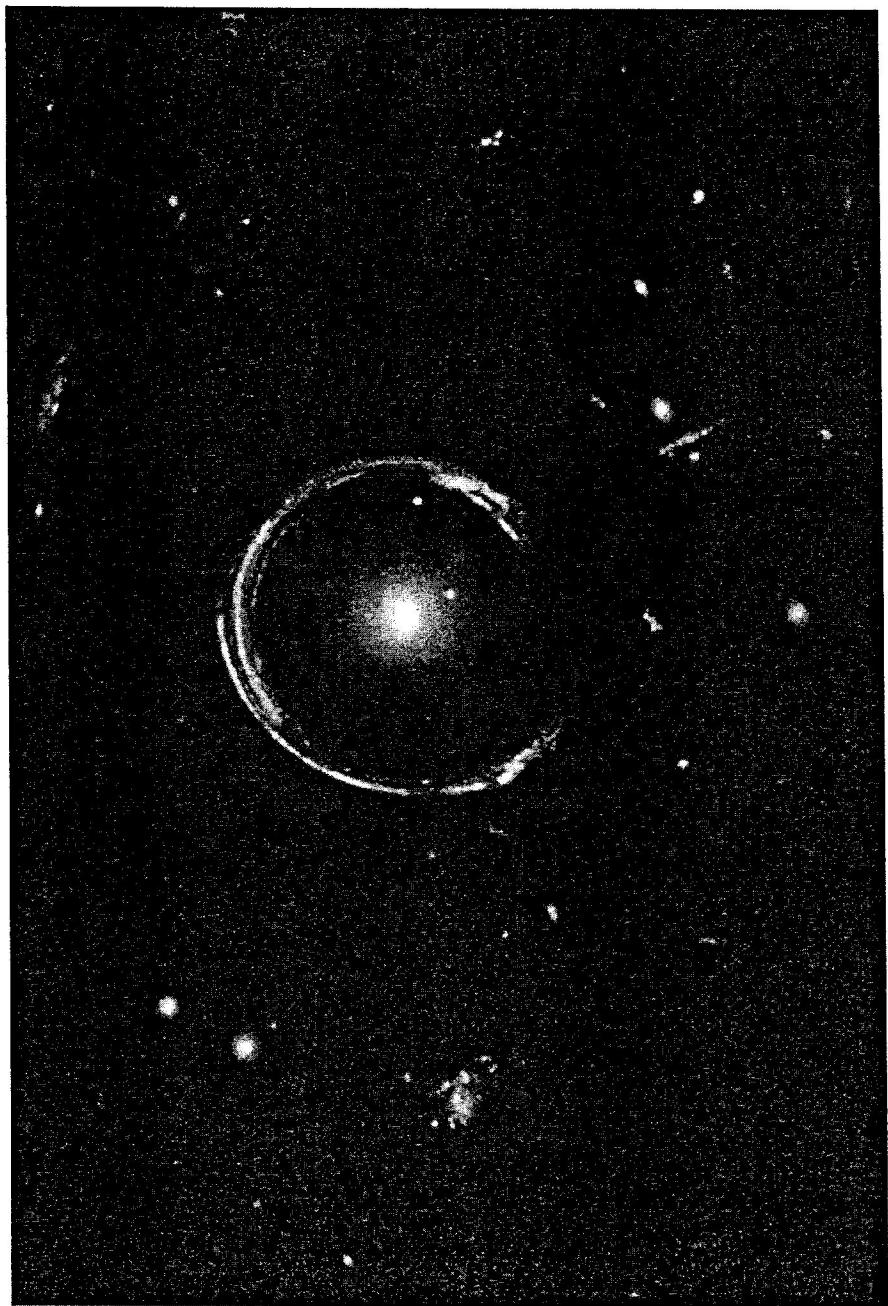
Gravitational Lensing in Observational Astronomy

- light from distant quasars bends around intermediate galaxy



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Gravitational Lensing in Observational Astronomy



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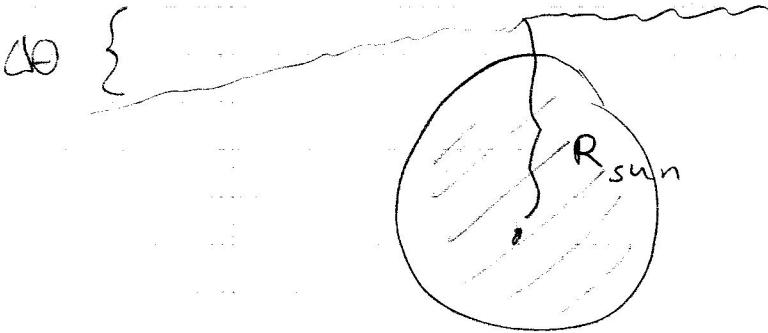


Gravitational Lens in Abell 2218 HST • WFPC2

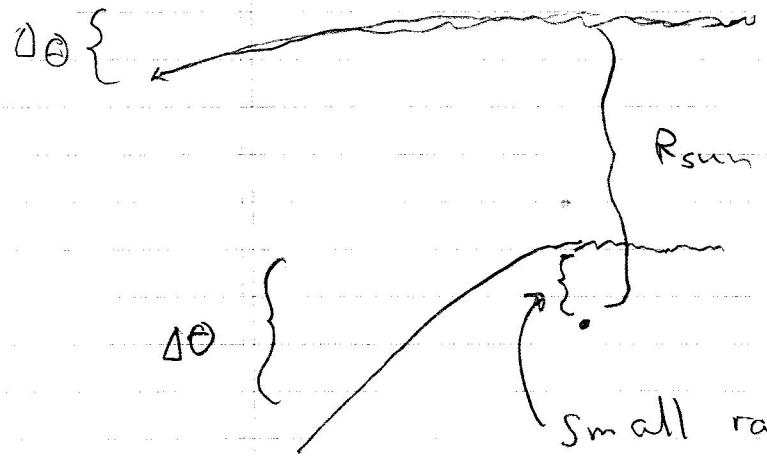
source – [Wikimedia](#)

Black Holes

Imagine you could contract the sun to a small point.



Then, as Newton taught us the force is the same.



Further, the deflection of light at a given radius is the same.

But, you can send the light much closer to the force center.

The angle gets larger.

Eventually, when

the radius is smaller than a certain

radius $R_{\text{Sch}} = \text{Schwarzschild Radius}$, the

angle becomes of order 90° and

the light doesn't escape



R_{sch} , light can not escape from this inner circle

Let's estimate the Schwarzschild radius
From before:

$$\Delta\theta \sim \frac{GM}{c^2 R}$$

↗ deflection

↖ how close we get
to sun
Schwarzschild

We can estimate the radius by setting the angle to

$$90^\circ = \frac{\pi}{2} \text{ rad}$$

S_0

$$\frac{\pi}{2} \sim \frac{GM}{c^2 R_{\text{sch}}}$$

$$R_{\text{sch}} \sim \frac{GM}{c^2 (\pi/2)}$$

Actual General Relativistic Corrections show that

$$R_{\text{sch}} = \frac{2GM}{c^2}$$