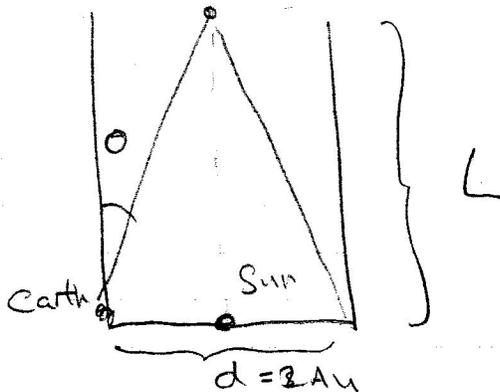


## Last Time:

### ① Measurement of Distances using Parallax



$$\theta \approx \frac{d/2}{L}$$

$$L = \frac{d/2}{\theta} \rightarrow \text{for } d = 1 \text{ Au} \quad L = \frac{1 \text{ Au}}{\theta}$$

So this can be used to measure distances if angles can be measured precisely

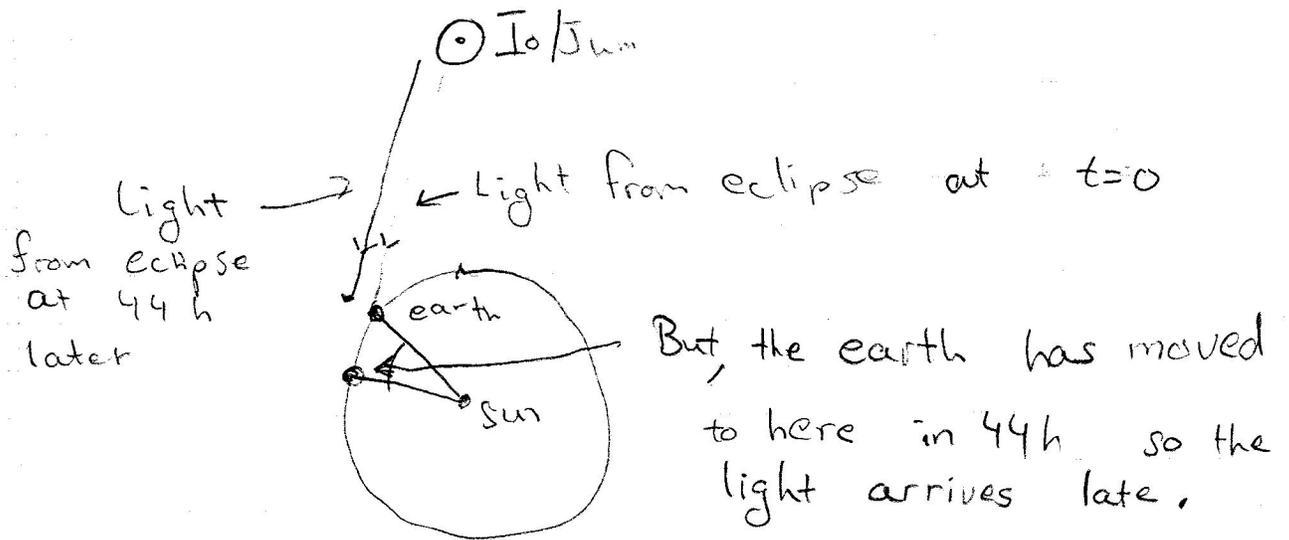
- Used to establish the distance to nearest stars

$\alpha$ -centauri  $\sim 4.1 \text{ y}$

- Currently still used to calibrate known sources (discussed today)

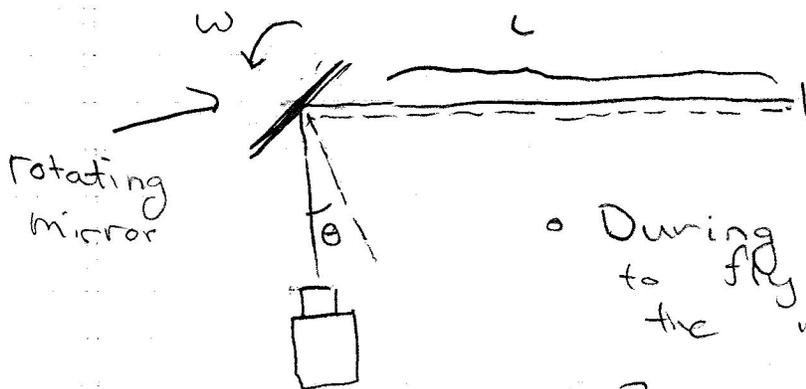
- Hipparcos satellite measures distances  
① parallax to  $\sim 300 \text{ y}$

② Then we started to discuss the speed of light; (Roemer)



So found,  $c = (3 \times 10^8 \text{ m/s})$

Then, Later earth based measurements  
Fizeau & Foucault ~ 1862



• During the time it takes to fly down and back the mirror rotates

• By measuring the angle, and knowing the distance  $L$ , and the rotation rate  $\omega$ , find  $c$ .

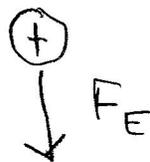
$$2.99 \times 10^8 \text{ m/s}$$

### ③ Relativity

→ A built in property of Electricity and magnetism



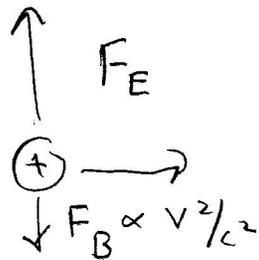
This is A's point of view



A:



B: ←



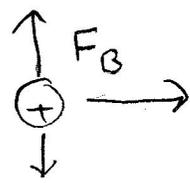
This is B's point of view,

• According to B the charges are moving

and therefore there

is a small magnetic attraction

A:



B:



Einstein's Answer - Both A & B measure different forces, but they also measure different accelerations. The laws of physics are the same for all

$$m \frac{\Delta v_A}{\Delta t_A} = F_A$$

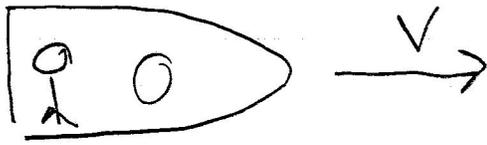
Similarly

$$m \frac{\Delta v_B}{\Delta t_B} = F_B$$

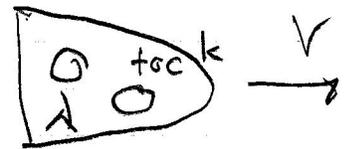
But  $F_A \neq F_B$  and similarly  $\Delta t_A \neq \Delta t_B$   
and similarly  $\Delta v_A \neq \Delta v_B$

Have no fear Einstein tells you  
how to relate  $\Delta t_A$  and  $\Delta t_B$

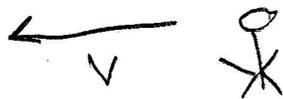
# Time Dilation



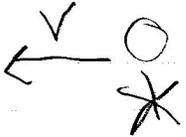
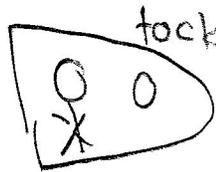
The Ground Observer sees the clock moving



The space ship sees



Then later



- Then according to spaceship the time interval occurred at the same point. We call this a proper time interval, call it  $\Delta\tau$ .
- For the ground observer tick and tock happen at different points and is not a proper time interval, call it  $\Delta t$ .

The relation between  $\Delta t$  and  $\Delta\tau$  is

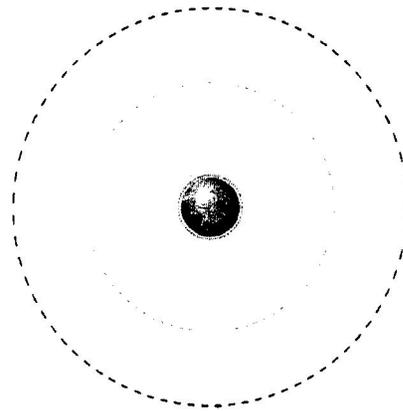
$$\Delta t = \gamma \Delta\tau$$

Where

$$\gamma = \frac{1}{(1 - (v/c)^2)^{1/2}}$$

## Group work II.

- A clock in a satellite is orbiting 200 km above the earth in a low earth orbit. The region of low earth orbit is shown below (to scale) as the cyan (or blue) region. (Neglect the differences in gravity between the earth observer and the satellite since the orbit is low. We will discuss the the gravitational differences today)



1. Determine the orbital period according using Kepler's Law,  $\Delta t_{\text{earth}}$ .
2. Determine the speed of the satellite
3. After orbiting once, the clock in the satellite and on earth read different times, which shows a longer elapsed time.
4. Compute

$$\frac{\Delta t_{\text{earth}} - \Delta t_{\text{sat}}}{\Delta t_{\text{earth}}} = 1 - \frac{\Delta t_{\text{earth}}}{\Delta t_{\text{sat}}}$$

5. You will need a lot of digits (about 13) when computing  $\gamma = 1/\sqrt{1 - (v/c)^2}$ . Go to [www.wolframalpha.com](http://www.wolframalpha.com)

Now Lets Review the Material (General Relativity)  
from two lectures ago.

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① The principle of equivalence  
(see slides)

② Light is Bent as it goes  
past a massive Body

$$\Delta\theta \sim \frac{GM}{c^2 R} \Rightarrow \boxed{\Delta\theta = \frac{4GM}{c^2 R}}$$

↙ exact

In particular for light passing near  
the sun

$$M = M_{\odot} \quad R = R_{\odot}$$

$\Delta\theta = 1.73$  arcsec -- Measured by the  
Eddington expedition.

③ If an object is sufficiently massive  
at a fixed size, then light will not  
be able to escape from a radius

known as the Schwarzschild radius

$$R_{\text{sch}} \sim \frac{GM}{c^2} \Rightarrow \boxed{R_{\text{sch}} = \frac{2GM}{c^2}}$$

④ Due to the finite speed of light Mercury's Elliptic orbit will precess

$$\frac{\Delta\theta}{\Delta t} \sim 43 \text{ arcsec/century}$$

⑤ In the presence of strong gravitational fields there is gravitational lensing of light

⑥ Today we will add one more test of GR known as the gravitational red-shift.