- 1. Principle of Equivalence
- 2. Bending of Light

$$\Delta \theta = \frac{4GM}{c^2R}$$
 or $\Delta \theta = 1.76\,\mathrm{arcsec}$ for light near sun

- 3. Gravitational Lensing
- 4. Black Holes light can not escape for $R < R_{
 m sch}$

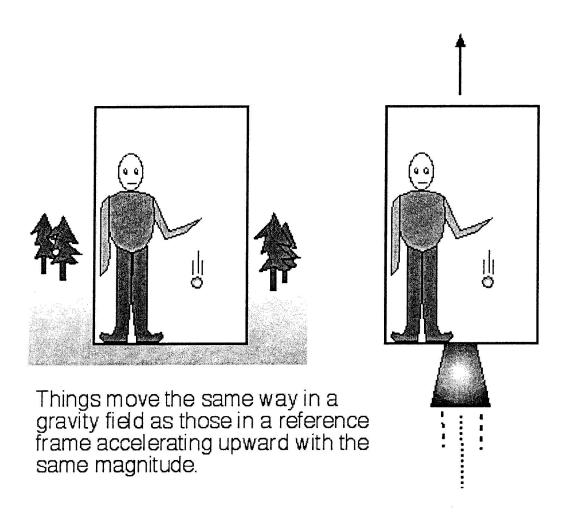
$$R_{\rm sch} = \frac{2GM}{c^2}$$

5. Precession of Perihelion of Mercury – see here. The GR contribution is

$$\frac{\Delta \theta}{\Delta t} \sim \frac{360^o}{88\,\mathrm{days}} \left(\frac{v}{c}\right)^2$$
 exact calculation gives $\frac{\Delta \theta}{\Delta t} \simeq 43\,\mathrm{arcsec/century}$

Equivalence Principle

• There is no experiment a person could conduct (in a small volume) that can distinguish gravitational forces from accelerated motion.



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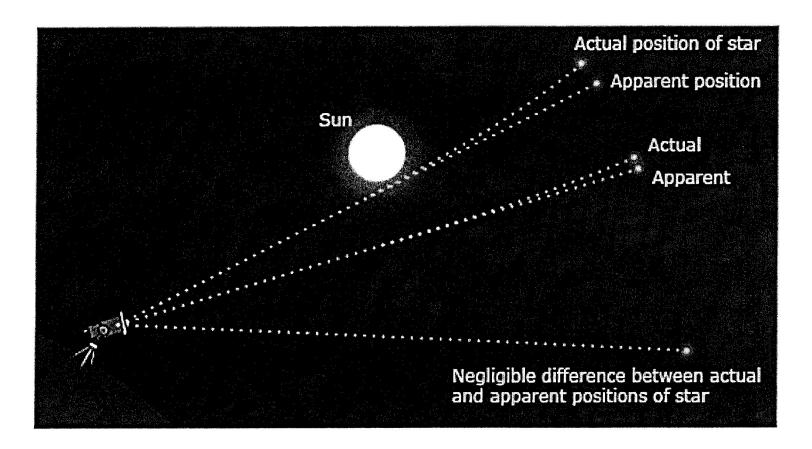
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Measuring the bending of light

- Measure the deflection of starlight as it goes near the sun
- Compare angles between the stars during a solar eclipse,
 and at night at a different time of the year



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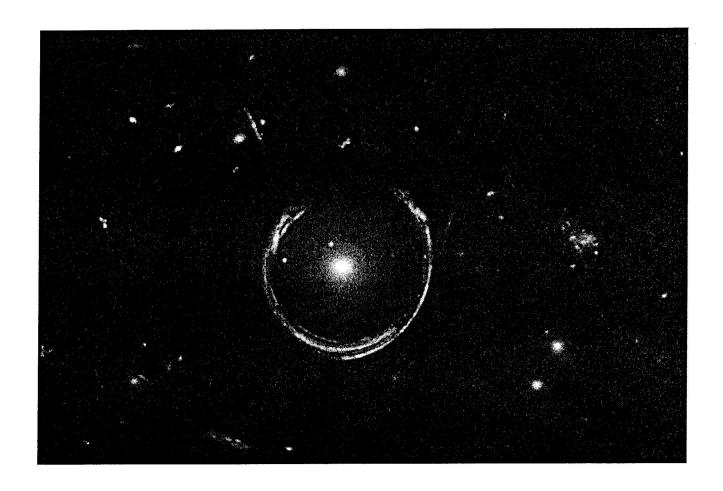
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Gravitational Lensing in Observational Astronomy



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6. Today. Gravitational Red-shift experiment and application to GPS.