

Problems:

1. An unstable particle having a mass of $m_{\text{parent}} = 3.34 \times 10^{-27}$ kg is initially at rest. The particle decays into two fragments that fly off with velocities of $0.987 c$ and $-0.868 c$. Find the rest masses of the fragments. Give your result in a formula before putting in numbers.
2. The average power generated by the Sun has the value 3.74×10^{26} W.
 - i) Assuming the average wavelength of the Sun's radiation to be 500 nm, find the number of photons emitted by the Sun in 1 s.
 - ii) Assuming the average temperature on the surface of the sun to be 5800 K, find the number of photons emitted by the Sun in 1 s. (Hint: assume that the Sun radiates like a black body, and make use of the formula derived in problem 2 of the last homework.)
3. A light source of wavelength λ illuminates a metal and ejects photoelectrons with a maximum kinetic energy of 1.00 eV. A second light source with half the wavelength of the first ejects photoelectrons with a maximum kinetic energy of 4.00 eV. What is the work function A of the metal? What is the wavelength λ ?
4. Johann Jakob Balmer, a Swiss schoolteacher, found by trial and error in 1885 a pocket formula for the wavelengths of spectral lines in hydrogen

$$\lambda = C_2 \left(\frac{n^2}{n^2 - 2^2} \right),$$

where $C_2 = 3645.6 \times 10^{-8}$ cm.

- i) Show that Balmer's formula is a special case of the Rydberg formula, given in eq. (3.13) of the lecture notes. What is the value of n_f for the Balmer series? Calculate the first three lines in the Balmer series of hydrogen.
- ii) The Lyman series describes the spectral lines of the hydrogen atoms for transitions to the ground state $n_f = 1$. Calculate the first three lines in the Lyman series of hydrogen. Are these lines in the visible, ultraviolet or infrared part of the spectrum?
5. A hydrogen atom initially in its ground state ($n=1$) absorbs a photon and ends up in the state for which $n=3$.
 - i) What is the energy of the absorbed photon in units of eV?
 - ii) If the atom returns to the ground state, what photon energies could the atom emit? (Hint: there is more than one energy!)
6. i) Find the energy of an x-ray photon that can impart a maximum energy of 50 keV to an electron by Compton collision.
 - ii) Compton used photons of wavelength 0.0711 nm. What is the energy of these photons? What is the wavelength of the photons scattered at an angle of 180° (backscattering case)? What is the energy of the backscattered photons? What is the recoil energy of the electrons in the backscattering case?